

## *Chemical Equilibrium*

*Dr. Ron Rusay*



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## *Chemical Equilibrium*

- *The reactions considered until now have had reactants react completely to form products. These reactions “went” only in one direction.*
- *Some reactions can react in either direction. They are “reversible”. When this occurs some amount of reactant(s) will always remain in the final reaction mixture.*

## *Chemical Equilibrium*

*(Definitions)*

- *A chemical system where the concentrations of reactants and products remain constant over time.*
- *On the molecular level, the system is dynamic: The rate of change is the same in either the forward or reverse directions.*

## *Dynamic Equilibrium*

*“The Pennies”*

- *Organize into groups of 4.*
- *Dr. R will provide your group with a number and an accounting form.*
- *In your group, select one person as:*
  - 1) *Money Keeper*
  - 2) *Recorder*
  - 3) *Transfer Agent*
  - 4) *Auditor*
- *Have the Recorder put everyone’s name on the accounting form.*
- *After recording all of the names send the Money Keeper to see Dr. R. for your capital stake.*
- *Await instructions for phase I.*

## Dynamic Equilibrium "The Pennies"

There will be 8 phases. Find your Equilibrium trading partners eg. IA with IB, IIA with IIB, etc. Below it is illustrated as 1X with 1Y and 2X and 2Y.

Phase I:

Group	1 X	1 Y	2 X	2 Y
Rate	-30%	-10%	-30%	-50%
initial	40	0	20	20
change				
final				

Phase II:

initial				
change				
final				

## Dynamic Equilibrium "The Pennies"

Phase I below illustrates 1 X starting with 40 pennies and giving 12(50%) to 1 Y who has 0 pennies and has none to give 10% of; 2 X starts with 20 and gives 6(30%) to 2 Y while 2Y also starts with 20 but gives only 10(50%) to 2X.

Phase I:

Group	1 X	1 Y	2 X	2 Y
Rate	-30%	-10%	-30%	-50%
initial	40	0	20	20
change	-12	+12	-6+10	-10+6
final				

Phase II:

initial				
change				
final				

## Dynamic Equilibrium "The Pennies"

Phase I ends with a closing balance illustrated in red and a net change of -12 for 1X, +12 for 1Y; +4 for 2X and -4 for 2Y

Phase I:

Group	1 X	1 Y	2 X	2 Y
Rate	-30%	-10%	-30%	-50%
initial	40	0	20	20
change	-12	+12	-6+10	-10+6
final	28	12	24	16

Phase II:

initial				
change				
final				

## Dynamic Equilibrium "The Pennies"

Phase II starts with the balance from Phase I

Phase I:

Group	1 X	1 Y	2 X	2 Y
Rate	-30%	-10%	-30%	-50%
initial	40	0	20	20
change	-12	+12	-6+10	-10+6
final	28	12	24	16
Rate	-30%	-10%	-25%	-50%
initial	28	12	24	16
change				
final				

Phase II:

initial				
change				
final				

Calculate the change and final amounts for your Phase I, which is the initial amount for Phase II. Once you are ready, you can begin and go through Phases 1-4 at your own pace. Stop after Phase 4 and await further instructions..

## Pennies Results

	IA	IB	IIA	IBB	IIIA	IIIB	IVIA	IVB
initial	-50%	-10%	-25%	-50%	-10%	-50%	-50%	-25%
final	4.0	0	2.0	2.0	2.0	2.0	0	4.0
change	2.0	2.0	2.5	1.5	2.0	1.2	1.0	3.0
initial	-50%	-10%	-25%	-50%	-10%	-50%	-50%	-25%
change	1.2	2.0	2.0	1.3	3.1	9	1.2	2.8
final	-50%	-10%	-25%	-50%	-10%	-50%	-50%	-25%
change	9	3.1	2.7	1.4	3.3	7	1.3	2.7
initial	-50%	-10%	-25%	-50%	-10%	-50%	-50%	-25%
change	3	3.3	2.7	1.4	3.6	6	1.3	2.7
final								
initial	-25%	-50%	-50%	-10%	-50%	-25%	-10%	-50%
change	2.2	1.8	1.4	2.6	1.9	2.1	2.5	1.5
final	-25%	-50%	-50%	-10%	-50%	-25%	-10%	-50%
change	2.3	1.5	1.0	3.0	1.4	2.6	3.0	1.0
initial	-25%	-50%	-50%	-10%	-50%	-25%	-10%	-50%
change	2.3	1.9	8	3.2	1.4	3.4	3.2	3
initial	-25%	-50%	-50%	-10%	-50%	-25%	-10%	-50%
change	3.7	1.9	7	3.3	1.4	2.6	3.3	3
final								

## Dynamic Equilibrium "The Pennies"

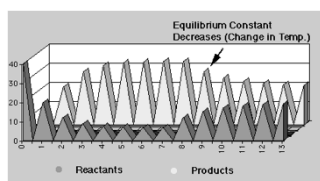
### Class Results

<http://chemconnections.org/general/chem120/equil-graph.html>

### Simulator:

<http://chemconnections.org/Java/equilibrium/>

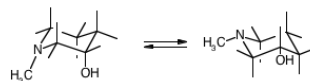
## Dynamic Equilibrium "The Pennies"



<http://chemconnections.org/general/chem120/equil-graph.html>

## Chemical Equilibrium

• Consider  $A \rightleftharpoons B$

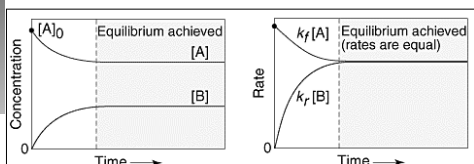


[Refer to the Equilibrium Worksheet.]

- If the reaction begins with just A, as the reaction progresses:
  - [A] decreases to a constant concentration,
  - [B] increases from zero to a constant concentration.
  - When [A] and [B] are constant, equilibrium is reached.

## Chemical Equilibrium

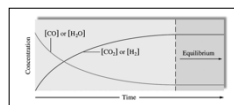
Graphical Treatment of Rates & Changes



- Rate of loss of  $A = -k_f[A]$ ; decreases to a constant,
- Rate of formation of  $B = k_r[B]$ ; increases from zero to a constant.
- When  $-k_f[A] = k_r[B]$  equilibrium is reached.

## QUESTION

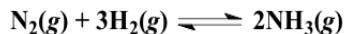
The changes in concentrations with time for the reaction  $\text{H}_2\text{O}(\text{g}) + \text{CO}(\text{g}) \rightleftharpoons \text{H}_2(\text{g}) + \text{CO}_2(\text{g})$  are graphed below when equimolar quantities of  $\text{H}_2\text{O}(\text{g})$  and  $\text{CO}(\text{g})$  are mixed.



Which of the comments given here accurately apply to the concentration versus time graph for the  $\text{H}_2\text{O} + \text{CO}$  reaction?

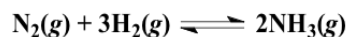
- The point where the two curves cross shows the concentrations of reactants and products at equilibrium.
- The slopes of tangent lines to each curve at a specific time prior to reaching equilibrium are equal, but opposite, because the stoichiometry between the products and reactants is all 1:1.
- Equilibrium is reached when the  $\text{H}_2\text{O}$  and  $\text{CO}$  curves (green) get to the same level as the  $\text{CO}_2$  and  $\text{H}_2$  curves (red) begin.
- The slopes of tangent lines to both curves at a particular time indicate that the reaction is fast and reaches equilibrium.

## Chemical Equilibrium



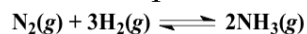
- Add nitrogen and hydrogen gases together in any proportions. Nothing noticeable occurs.
- Add heat, pressure and a catalyst, you smell ammonia  $\Rightarrow$  a mixture with constant concentrations of  $\text{N}_2$ ,  $\text{H}_2$  and  $\text{NH}_3$  is produced.
- Start with just ammonia and catalyst.  $\text{N}_2$  and  $\text{H}_2$  will be produced until a state of equilibrium is reached.
- As before, a mixture with constant concentrations of nitrogen, hydrogen and ammonia is produced.

## Chemical Equilibrium

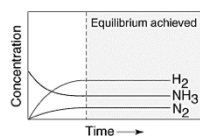
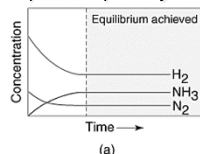


No matter what the starting composition of reactants and products, the same ratio of concentrations is realized when equilibrium is reached at a certain temperature and pressure.

## Chemical Equilibrium

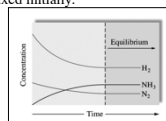


The Previous Examples Graphically:



## QUESTION

This is a concentration profile for the reaction  $\text{N}_2(\text{g}) + 3\text{H}_2(\text{g}) \rightleftharpoons 2\text{NH}_3(\text{g})$  when only  $\text{N}_2(\text{g})$  and  $\text{H}_2(\text{g})$  are mixed initially.



The figure shown here represents the concentration versus time relationship for the synthesis of ammonia ( $\text{NH}_3$ ). Which of the following correctly interprets an observation of the system?

- At equilibrium, the concentration of  $\text{NH}_3$  remains constant even though some is also forming  $\text{N}_2$  and  $\text{H}_2$ , because some  $\text{N}_2$  and  $\text{H}_2$  continues to form  $\text{NH}_3$ .
- The  $\text{NH}_3$  curve (red) crosses the  $\text{N}_2$  curve (blue) before reaching equilibrium because it is formed at a slower rate than  $\text{N}_2$  rate of use.
- All slopes of tangent lines become equal at equilibrium because the reaction began with no product ( $\text{NH}_3$ ).
- If the initial  $\text{N}_2$  and  $\text{H}_2$  concentrations were doubled from what is shown here, the final positions of those curves would be twice as high, but the  $\text{NH}_3$  curve would be the same.

## Law of Mass Action

(Equilibrium Expression)

- For a reaction:
  - $j\text{A} + k\text{B} \rightleftharpoons l\text{C} + m\text{D}$
- The law of mass action is represented by the Equilibrium Expression: where  $K$  is the Equilibrium Constant. (Units for  $K$  will vary.)

$$K = \frac{[\text{C}]^l [\text{D}]^m}{[\text{A}]^j [\text{B}]^k}$$

## QUESTION

One of the environmentally important reactions involved in acid rain production has the following equilibrium expression.

From the expression, what would be the balanced chemical reaction?

Note: all components are in the gas phase.

$$K = \frac{[\text{SO}_3]}{[\text{SO}_2][\text{O}_2]^{1/2}}$$

- $\text{SO}_3(\text{g}) \rightleftharpoons \text{SO}_2(\text{g}) + 2\text{O}_2(\text{g})$
- $\text{SO}_3(\text{g}) \rightleftharpoons \text{SO}_2(\text{g}) + 1/2\text{O}_2(\text{g})$
- $\text{SO}_2(\text{g}) + 2\text{O}_2(\text{g}) \rightleftharpoons \text{SO}_3(\text{g})$
- $\text{SO}_2(\text{g}) + 1/2\text{O}_2(\text{g}) \rightleftharpoons \text{SO}_3(\text{g})$

### Equilibrium Expression

- $4 \text{NH}_3(\text{g}) + 7 \text{O}_2(\text{g}) \leftrightarrow 4 \text{NO}_2(\text{g}) + 6 \text{H}_2\text{O}(\text{g})$
- Write the Equilibrium Expression for the reaction. The expression will have either concentration units of mol/L (M), or units of pressure (atm) for the reactants and products. What would be the overall unit for K using Molarity and atm units respectively.

$$K = \frac{[\text{NO}_2]^4 [\text{H}_2\text{O}]^6}{[\text{NH}_3]^4 [\text{O}_2]^7}$$

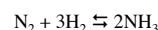
*K's units =  $\text{M}^{-1} = \text{L/mol}$  or  $\text{atm}^{-1}$*

## QUESTION

Starting with the initial concentrations of:

$$[\text{NH}_3] = 2.00 \text{ M}; [\text{N}_2] = 2.00 \text{ M}; [\text{H}_2] = 2.00 \text{ M},$$

what would you calculate as the equilibrium ratio once the equilibrium position is reached for the ammonia synthesis reaction?



- A.1.00
- B.0.250
- C.4.00
- D.This cannot be done from the information provided.

### Equilibrium Expressions

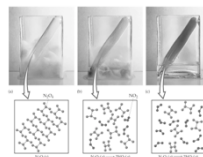
- 1) If a reaction is re-written where the reactants become products and products-reactants, the new Equilibrium Expression is the reciprocal of the old.

$$K_{\text{new}} = 1 / K_{\text{original}}$$

- 2) When the entire equation for a reaction is multiplied by n,

$$K_{\text{new}} = (K_{\text{original}})^n$$

### The Equilibrium Constant



$$K_c = \frac{[\text{NO}_2]^2}{[\text{N}_2\text{O}_4]} \quad \boxed{\phantom{0.000}}$$

Initial and Equilibrium Partial Pressures (P) of N <sub>2</sub> O <sub>4</sub> and NO <sub>2</sub> at 100 °C					
Experiment	Initial N <sub>2</sub> O <sub>4</sub> Partial Pressure (atm)	Initial NO <sub>2</sub> Partial Pressure (atm)	Equilibrium N <sub>2</sub> O <sub>4</sub> Partial Pressure (atm)	Equilibrium NO <sub>2</sub> Partial Pressure (atm)	K <sub>eq</sub>
1	0.0	0.612	0.0429	0.526	6.45
2	0.0	0.919	0.0857	0.744	6.46
3	0.0	1.22	0.138	0.944	6.46
4	0.612	0.0	0.138	0.944	6.46

## The Equilibrium Constant



$$K_{\text{eq}} = \frac{(P_{\text{NO}_2})^2}{(P_{\text{N}_2\text{O}_4})} \quad \text{and} \quad K_{\text{eq}} = \frac{(P_{\text{N}_2\text{O}_4})}{(P_{\text{NO}_2})^2}$$

Since their equilibrium expressions are reciprocal to one another, their equilibrium constants are also reciprocals. Point to each expression to see its numerical value at 10°C.

## The Equilibrium Constant



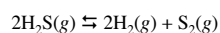
$$K_c = \frac{[\text{NO}_2]^2}{[\text{N}_2\text{O}_4]} = 0.212$$



$$K_c = \frac{[\text{N}_2\text{O}_4]}{[\text{NO}_2]^2} = \frac{1}{0.212} = 4.72$$

## QUESTION

One of the primary components in the aroma of rotten eggs is  $\text{H}_2\text{S}$ . At a certain temperature, it will decompose via the following reaction.

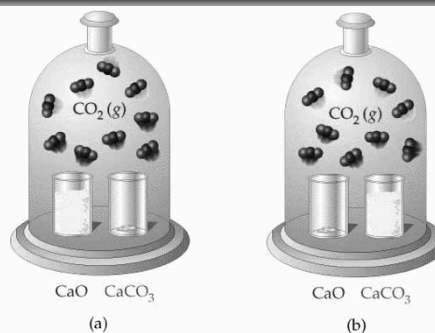


If an equilibrium mixture of the gases contained the following pressures of the components, what would be the value of  $K_p$ ?

$$P_{\text{H}_2\text{S}} = 1.19 \text{ atm}; P_{\text{H}_2} = 0.25 \text{ atm}; P_{\text{S}_2} = 0.25 \text{ atm}$$

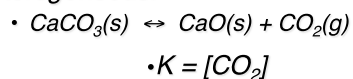
- A. 0.011
- B. 91
- C. 0.052
- D. 0.013

## Heterogeneous Equilibrium



### Heterogeneous Equilibria

- When all reactants and products are in one phase, the equilibrium is homogeneous.
- If one or more reactants or products are in a different phase, the equilibrium is heterogeneous.



### Heterogeneous Equilibria

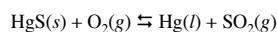


$$K = [\text{CO}_2]$$

- Experimentally, the amount of  $\text{CO}_2$  does not meaningfully depend on the amounts of  $\text{CaO}$  and  $\text{CaCO}_3$ .
- The position of a heterogeneous equilibrium does not depend on the amounts of pure solids or liquids present.

### QUESTION

The liquid metal mercury can be obtained from its ore cinnabar via the following reaction:

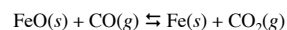


Which of the following shows the proper expression for  $K_c$ ?

- A.  $K_c = [\text{Hg}][\text{SO}_2]/[\text{HgS}][\text{O}_2]$
- B.  $K_c = [\text{SO}_2]/[\text{O}_2]$
- C.  $K_c = [\text{Hg}][\text{SO}_2]/[\text{O}_2]$
- D.  $K_c = [\text{O}_2]/[\text{SO}_2]$

### QUESTION

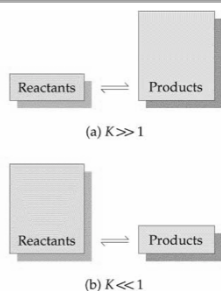
At a certain temperature, FeO can react with CO to form Fe and  $\text{CO}_2$ . If the  $K_p$  value at that temperature was 0.242, what would you calculate as the pressure of  $\text{CO}_2$  at equilibrium if a sample of FeO was initially in a container with CO at a pressure of 0.95 atm?



- A. 0.24 atm
- B. 0.48 atm
- C. 0.19 atm
- D. 0.95 atm

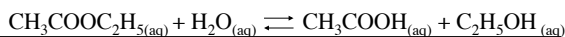


## The Equilibrium Constant $K$



## Calculating Equilibrium Constants

- Tabulate 1) initial and 2) equilibrium concentrations (or partial pressures).
- Having both an initial and an equilibrium concentration for any species, calculate its change in concentration.
- Apply stoichiometry to the change in concentration to calculate the changes in concentration of all species.
- Deduce the equilibrium concentrations of all species.



$K_c$ : 5.00 ml of ethyl alcohol, 5.00 ml of acetic acid and 5.00 ml of 3M hydrochloric acid were mixed in a vial and allowed to come to equilibrium. The equilibrium mixture was titrated and found to contain 0.04980 mol of acetic acid at equilibrium. What is the value of  $K_c$ ?

- 1) Calculate the initial molar concentrations (moles are OK in this case).
- 2) Use the equilibrium concentration of acetic acid to determine the changes and the equilibrium concentrations of the others.
- 3) Place the equilibrium values into the equilibrium expression to find it's value.

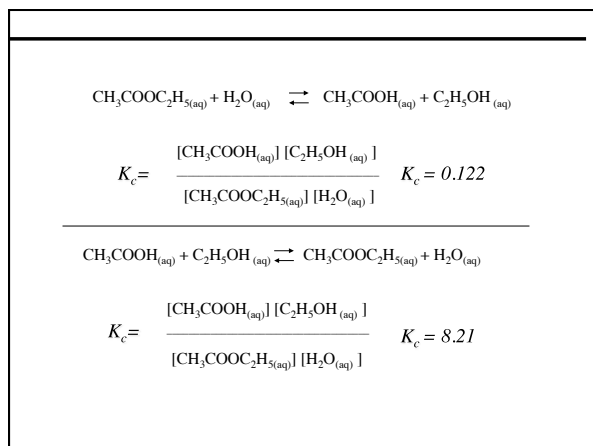
	$\text{CH}_3\text{COOC}_2\text{H}_5(\text{aq})$	$+\text{H}_2\text{O}(\text{aq})$	$\rightleftharpoons$	$\text{CH}_3\text{COOH}(\text{aq})$	$+\text{C}_2\text{H}_5\text{OH}(\text{aq})$
Initial (mol)	0	0.261		0.0873	0.0856
Change	+0.0375	+0.0375		-0.0375	-0.0375
Equilibrium	0.0375	0.2985		0.0498	0.0481
				$0.0873 - 0.0498 = 0.0375$	

$K_c = 0.214$

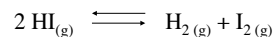
## Calculating Equilibrium Constants

- 1) Write the Equilibrium Expression for the hydrolysis of ethyl acetate and calculate  $K_c$  from the following equilibrium concentrations.
- 2) Write the Equilibrium Expression for the formation of ethyl acetate from acetic acid and calculate  $K_c$  from the following equilibrium concentrations.

Ethyl acetate = 0.01217 M; Ethanol = 0.01623 M  
Acetic acid = 0.01750 M ; Water = 0.09267 M



### Calculating $K_c$ from Concentration Data



4.00 mol HI was placed in a 5.00 L vessel at 458°C, the equilibrium mixture was found to contain 0.442 mol  $\text{I}_2$ . What is the value of  $K_c$ ? Calculate the molar concentrations, and put them into the equilibrium expression to find its value.

$$\text{Initial conc. of HI} = \frac{4.00 \text{ mol}}{5.00 \text{ L}} = 0.800 \text{ M}$$

$$\text{Equilibrium conc. of } \text{I}_2 = \frac{0.442 \text{ mol}}{5.00 \text{ L}} = 0.0884 \text{ M}$$

Conc. (M)	$2\text{HI}_{(\text{g})}$	$\rightleftharpoons$	$\text{H}_{2(\text{g})}$	$\text{I}_{2(\text{g})}$
Initial	0.800		0	0
Change	- 2x		x	x
Equilibrium	0.800 - 2x		x	x = 0.0884

### Calculating $K_c$ from Concentration Data (continued)



$$[\text{HI}] = M = (0.800 - 2 \times 0.0884) \text{ M} = 0.623 \text{ M}$$

$$[\text{H}_2] = x = 0.0884 \text{ M} = [\text{I}_2]$$

$$K_c = \frac{[\text{H}_2][\text{I}_2]}{[\text{HI}]^2} = \frac{(0.0884)(0.0884)}{(0.623)^2} = 0.0201$$

What does the value 0.0201 mean? Does the decomposition proceed very far under these temperature conditions?

**Note:** The initial concentrations, and one at equilibrium were provided. The others that were needed to calculate the equilibrium constant were deduced algebraically.

### Calculation of Equilibrium Concentrations

- The same steps used to calculate equilibrium constants are used.
- Generally, we do not have a number for the change in concentrations line.
- Therefore, we need to assume that x mol/L of a species is produced (or used).
- The equilibrium concentrations are given as algebraic expressions. Solution of a quadratic equation may be necessary.

Ⓞ Choose an example. Then click each one of the boxes to see the steps.

**Simple Example**

A 1.0 L flask is charged at 750 K with 2.00 moles each of H<sub>2</sub> and I<sub>2</sub>. Determine the equilibrium concentrations of H<sub>2</sub>, I<sub>2</sub>, and HI. (K<sub>c</sub> = 57)

**More Complex Example**

- Step 1. Write the balanced equation for the reaction.
- Step 2. Under the balanced equation, make a table that lists for each substance involved in the reaction:
  - A) The initial concentration
  - B) The change in concentration on going to equilibrium
  - C) The equilibrium concentration

In constructing the table, define x as the concentration (mol/L) of one of the substances that reacts on going to equilibrium.
- Step 3. Substitute the equilibrium concentration into the equilibrium equation for the reaction and solve for x. If you must solve a quadratic equation, choose the mathematical solution that makes sense of sense.
- Step 4. Calculate the equilibrium concentrations from the calculated value of x.
- Step 5. Check your results by substituting them into the equilibrium equation.

<http://chemconnections.org/general/chem120/UsinganEquilibriumTable11.swf>

## QUESTION

The weak acid HC<sub>2</sub>H<sub>3</sub>O<sub>2</sub>, acetic acid, is a key component in vinegar. As an acid the aqueous dissociation equilibrium could be represented as

$$\text{HC}_2\text{H}_3\text{O}_2(aq) \rightleftharpoons \text{H}^+(aq) + \text{C}_2\text{H}_3\text{O}_2^-(aq).$$

At room temperature the K<sub>c</sub> value, at approximately 1.8 × 10<sup>-5</sup>, is not large. What would be the equilibrium concentration of H<sup>+</sup> starting from 1.0 M acetic acid solution?

A. 1.8 × 10<sup>-5</sup> M  
 B. 4.2 × 10<sup>-3</sup> M  
 C. 9.0 × 10<sup>-5</sup> M  
 D. More information is needed to complete this calculation.

### Equilibrium Concentration Calculations from Initial Concentrations and K<sub>c</sub>

The reaction to form HF from hydrogen and fluorine has an equilibrium constant of 115 at temperature T. If 3.000 mol of each component is added to a 1.500 L flask, calculate the equilibrium concentrations of each species.

$$\text{H}_2(g) + \text{F}_2(g) \rightleftharpoons 2 \text{HF}(g)$$

**Solution:**

$$K_c = \frac{[\text{HF}]^2}{[\text{H}_2][\text{F}_2]} = 115$$

$$[\text{H}_2] = \frac{3.000 \text{ mol}}{1.500 \text{ L}} = 2.000 \text{ M}$$

$$[\text{F}_2] = \frac{3.000 \text{ mol}}{1.500 \text{ L}} = 2.000 \text{ M}$$

$$[\text{HF}] = \frac{3.000 \text{ mol}}{1.500 \text{ L}} = 2.000 \text{ M}$$

### Equilibrium Concentration Calculations

$$\text{H}_{2(g)} + \text{F}_{2(g)} \rightleftharpoons 2 \text{HF}_{(g)} \quad (\text{Continued})$$

Concentration (M)	H <sub>2</sub>	F <sub>2</sub>	HF
Initial	2.000	2.000	2.000
Change	-x	-x	+2x
Final	2.000-x	2.000-x	2.000+2x

$$K_c = \frac{[\text{HF}]^2}{[\text{H}_2][\text{F}_2]} = 115 = \frac{(2.000 + 2x)^2}{(2.000 - x)(2.000 - x)} = \frac{(2.000 + 2x)^2}{(2.000 - x)^2}$$

Taking the square root of each side:

$$(115)^{1/2} = \frac{(2.000 + 2x)}{(2.000 - x)} = 10.7238 \quad x = 1.528$$

$$[\text{H}_2] = 2.000 - 1.528 = 0.472 \text{ M}$$

$$[\text{F}_2] = 2.000 - 1.528 = 0.472 \text{ M}$$

$$[\text{HF}] = 2.000 + 2(1.528) = 5.056 \text{ M}$$

$$K_c = \frac{[\text{HF}]^2}{[\text{H}_2][\text{F}_2]} = \frac{(5.056 \text{ M})^2}{(0.472 \text{ M})(0.472 \text{ M})}$$

check: K<sub>c</sub> = 115

*Using the Quadratic Equation to solve for an unknown*

The gas phase reaction of 2 moles of CO and 1 mole of H<sub>2</sub>O in a 1L vessel:

Concentration (M)	CO <sub>(g)</sub>	+ H <sub>2</sub> O <sub>(g)</sub>	⇌	CO <sub>2(g)</sub>	+ H <sub>2(g)</sub>
Initial	2.00	1.00		0	0
Change	-x	-x		+x	+x
Equilibrium	2.00-x	1.00-x		x	x

$$K_c = \frac{[\text{CO}_2][\text{H}_2]}{[\text{CO}][\text{H}_2\text{O}]} = \frac{(x)(x)}{(2.00-x)(1.00-x)} = \frac{x^2}{x^2 - 3.00x + 2.00} = 1.56$$

We rearrange the equation:  $0.56x^2 - 4.68x + 3.12 = 0$   
 $ax^2 + bx + c = 0$

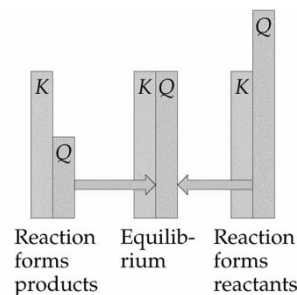
quadratic equation:

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$x = \frac{4.68 + \sqrt{(-4.68)^2 - 4(0.56)(3.12)}}{2(0.56)} = 7.6 \text{ M}$$

**[CO] = 1.27 M**  
**[H<sub>2</sub>O] = 0.27 M**  
**[CO<sub>2</sub>] = 0.73 M**  
**[H<sub>2</sub>] = 0.73 M**

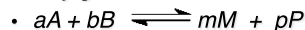
*Reaction Quotient (Q) vs. K*



*K vs. Q: Equilibrium Constants*

*Has equilibrium been reached?*

- Has equilibrium been reached? Q is the "reaction quotient" for any general reaction, for example:



$$Q = \frac{[\text{M}]^m [\text{P}]^p}{[\text{A}]^a [\text{B}]^b}$$

[A], [B], [P], and [M] are Molarities at any time.

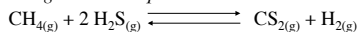
Q = K only at equilibrium

*Q vs. K: Predicting the Direction of Reaction*

- If  $Q < K$  then the forward reaction must occur to reach equilibrium. (i.e., reactants are consumed, products are formed, the numerator in the equilibrium constant expression increases and Q increases until it equals K).
- If  $Q > K$  then the reverse reaction must occur to reach equilibrium (i.e., products are consumed, reactants are formed, the numerator in the equilibrium constant expression decreases and Q decreases until it equals K).

### Calculating Reaction Direction and Equilibrium Concentrations

Two components of natural gas can react according to the following chemical equation:



1.00 mol  $\text{CH}_4$ , 1.00 mol  $\text{CS}_2$ , 2.00 mol  $\text{H}_2\text{S}$ , and 2.00 mol  $\text{H}_2$  are mixed in a 250 mL vessel at  $960^\circ\text{C}$ . At this temperature,  $K_c = 0.036$ .

(a) In which direction will the reaction go?

(b) If  $[\text{CH}_4] = 5.56 \text{ M}$  at equilibrium, what are the concentrations of the other substances?

Calculate  $Q_c$  and compare it with  $K_c$ . Based upon (a), we determine the sign of each component for the reaction table and then use the given  $[\text{CH}_4]$  at equilibrium to determine the others.

**Solution:**

$$[\text{CH}_4] = \frac{1.00 \text{ mol}}{0.250 \text{ L}} = 4.00 \text{ M} \quad [\text{H}_2\text{S}] = 8.00 \text{ M}, \quad [\text{CS}_2] = 4.00 \text{ M} \quad \text{and} \quad [\text{H}_2] = 8.00 \text{ M}$$

### Calculating Reaction Direction and Equilibrium Concentrations

$$Q_c = \frac{[\text{CS}_2][\text{H}_2]^4}{[\text{CH}_4][\text{H}_2\text{S}]^2} = \frac{4.00 \times (8.00)^4}{4.00 \times (8.00)^2} = 64.0$$

Compare  $Q_c$  and  $K_c$ :  $Q_c > K_c$  ( $64.0 > 0.036$ ), so the reaction goes to the left. Therefore, reactants increase and products decrease their concentrations.

(b) Set up the reaction table, with  $x = [\text{CS}_2]$  that reacts, which equals the  $[\text{CH}_4]$  that forms.

Concentration (M)	$\text{CH}_{4(g)}$	$+ 2 \text{H}_2\text{S}_{(g)}$	$\rightleftharpoons$	$\text{CS}_{2(g)}$	$+ 4 \text{H}_{2(g)}$
Initial	4.00	8.00		4.00	8.00
Change	+x	+2x		-x	-4x
Equilibrium	$4.00 + x$	$8.00 + 2x$		$4.00 - x$	$8.00 - 4x$

$$\text{Solving for } x \text{ at equilibrium: } [\text{CH}_4] = 5.56 \text{ M} = 4.00 \text{ M} + x \\ x = 1.56 \text{ M}$$

### Calculating Reaction Direction and Equilibrium Concentrations

$$x = 1.56 \text{ M} = [\text{CH}_4]$$

Therefore:

$$[\text{H}_2\text{S}] = 8.00 \text{ M} + 2x = 8.00 \text{ M} + 2(1.56 \text{ M}) = \mathbf{11.12 \text{ M}}$$

$$[\text{CS}_2] = 4.00 \text{ M} - x = 4.00 \text{ M} - 1.56 \text{ M} = \mathbf{2.44 \text{ M}}$$

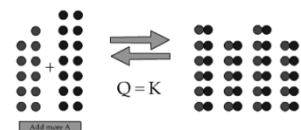
$$[\text{H}_2] = 8.00 \text{ M} - 4x = 8.00 \text{ M} - 4(1.56 \text{ M}) = \mathbf{1.76 \text{ M}}$$

$$[\text{CH}_4] = \mathbf{1.56 \text{ M}}$$

### Le Châtelier's Principle

- ... if a change is imposed on a system at equilibrium, the position of the equilibrium will shift in a direction that tends to reduce that change.

The pictures below represent the system  $\text{A} \rightleftharpoons 2\text{B}$  at equilibrium. A molecules are represented as red, B molecules are represented as blue. Click **Shift to A** button to stress the equilibrium.



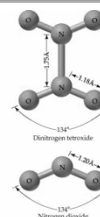
## Le Châtelier's Principle



Le Chatelier's Principle

## $NO_2 - N_2O_4$

$NO_2 \rightleftharpoons N_2O_4$  Equilibrium



## Temperature Dependence of $K$

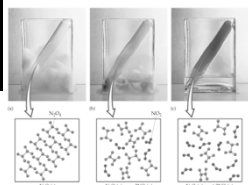
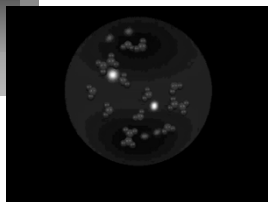
Nitrogen Dioxide and  
Dinitrogen Tetraoxide

Temperature Dependence  
of Equilibrium

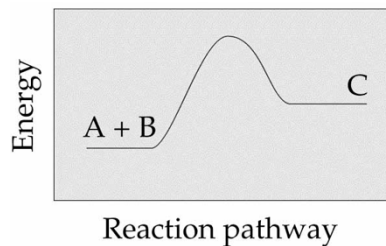
## Changes on the System

1. **Concentration:** The system will shift concentrations away from the added component.  $K$  remains the same.
2. **Temperature:**  $K$  changes depending upon the reaction.
  - If endothermic, heat is treated as a "reactant", if exothermic, heat is a "product". Endo-  $\rightarrow K$  increases; Exo-  $\rightarrow K$  decreases.
  - if  $\Delta H > 0$ , adding heat favors the forward reaction,
  - if  $\Delta H < 0$ , adding heat favors the reverse reaction.

## Chemical Equilibrium



Which is favored by raising the temperature in the following equilibrium reaction? A+B or C



## QUESTION

The following table shows the relation between the value of  $K$  and temperature of the system:

At 25°C;  $K = 45$ ; at 50°C;  $K = 145$ ; at 110°C;  $K = 467$

(a) Would this data indicate that the reaction was endothermic or exothermic? (b) Would heating the system at equilibrium cause more or less product to form?

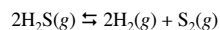
- A. Exothermic; less product
- B. Exothermic; more product
- C. Endothermic; less product
- D. Endothermic; more product

## Changes on the System (continued)

- 3. Pressure:
  - a. Addition of inert gas does not affect the equilibrium position.
  - b. Decreasing the volume shifts the equilibrium toward the side with fewer moles.
    - $K_p = K_c (RT)^{\Delta n}$
    - $\Delta n = n_{\text{gas}}(\text{products}) - n_{\text{gas}}(\text{reactants})$
- As the volume is decreased pressure increases.
- **Le Châtelier's Principle:** if pressure is increased the system shifts to minimize the increase.

## QUESTION

The balanced equation shown here has a  $K_p$  value of 0.011.  
What would be the value for  $K_c$  ?(at approximately 1,100°C)



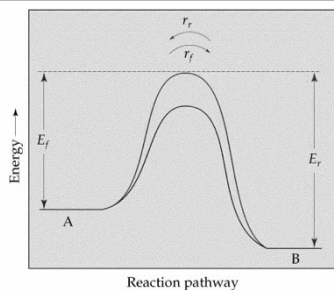
- A.0.000098
- B.0.011
- C.0.99
- D.1.2

## Changes on the System (continued)

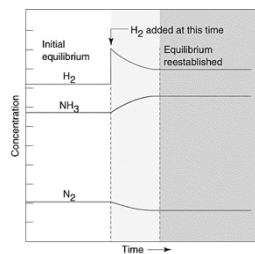
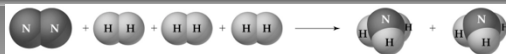
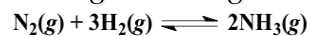
### 4. The Effect of Catalysts

- A catalyst lowers the activation energy barrier for any reaction....in both forward and reverse directions!
- A catalyst will decrease the time it takes to reach equilibrium.
- A catalyst **does not** effect the composition of the equilibrium mixture.

## Energy vs. Reaction Pathway

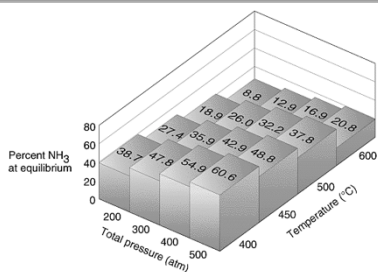


## Putting it all Together

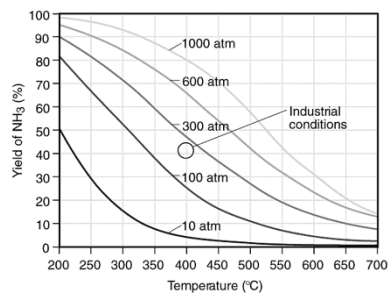




*Putting it all Together*  
 $N_2(g) + 3H_2(g) \rightleftharpoons 2NH_3(g)$



*Putting it all Together*  
 $N_2(g) + 3H_2(g) \rightleftharpoons 2NH_3(g)$



*Putting it all Together*  
 $N_2(g) + 3H_2(g) \rightleftharpoons 2NH_3(g)$

