

## Chemistry & STEM Measurement I

### Measurement, Conversions & Calculations Dr. Ron Rusay

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## CHEM 108 Basic Measurements: for stuff that you can see or sense

- LENGTH, WIDTH, HEIGHT, (DIAMETER)
- TIME
- VOLUME (occupied space)
- TEMPERATURE
- MASS (weight)

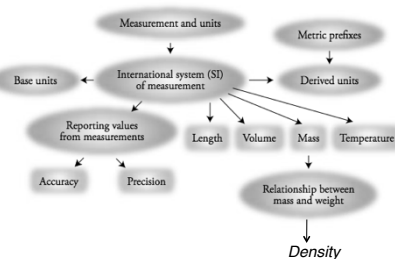
### • Qualitative vs. Quantitative

Eg. Qualitative: Old (sloth dung) vs.  
Young (you?)

Quantitative: 38,000 year old (dung) vs. a  
20 year old (you?)



## Units of Measure

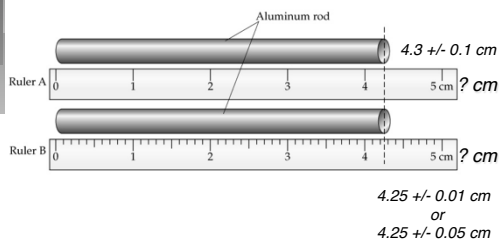


## Units of Measure

Base Units	U.S.	SI	Chemistry
Mass (weight)	Pound (lb)	Kilogram (kg)	"Gram" (g, mg) "Liter" (mL, L)
Volume	Gallon (gal)	Liter (L)	
Temperature	Fahrenheit (°F)	Kelvin (K)	K & Celsius (°C)
Length	Mile (mi), Feet (ft), Inches (in)	Meter (m)	"Meter" (cm, mm, nm)
Time		Second (s)	Second (s) Mole (mol)

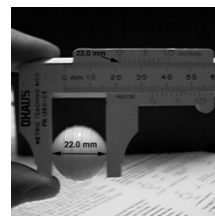
## What is the length of the rod?

Different measurement tools give different numbers:  
Which ruler is better?



## What is the diameter of a circle?

All measuring devices are not the same, and the values (numbers) that come from them indicate their limitations.



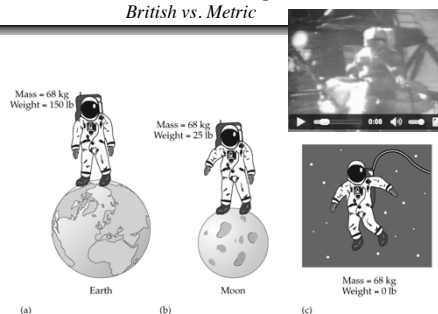
Is there a better instrument to use other than a ruler to  
measure the diameter of the sphere?

A caliper

## Mass Determination (Weighing Devices: Balances)



## Mass vs. Weight British vs. Metric



## Dimensional Analysis Conversion/Unit Factor Calculations

44.7 cm      ?      ? in  
information given × conversion factor(s) = information sought

$$\text{given unit} \times \frac{\text{desired unit}}{\text{given unit}} = \text{desired unit}$$

$$\frac{2.54 \text{ cm}}{1 \text{ in.}} = 1 = \frac{1 \text{ in.}}{2.54 \text{ cm}}$$

$$44.7 \text{ cm} \times \frac{1 \text{ in.}}{2.54 \text{ cm}} = 17.6 \text{ in.}$$



## Dimensional Analysis Conversion/Unit Factor Calculations

• *Qualitative Description: Are you heavy, slim, average? vs. Quantitative?.....The weight on your driver's license? birth certificate?*

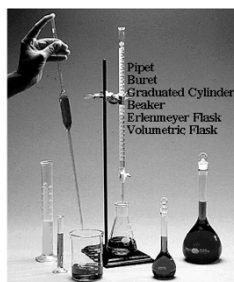
• *Calculate your weight in kilograms. Scale Factor*  
**UNITS:** 1 kg = 2.2 lb; 1 lb = 16 ounces (oz); 1 ounce (oz) = 0.0283495 kg

$$\text{? lbs} \quad \text{? ounces} \longrightarrow \text{? kg}$$

$$\begin{array}{c} \text{? lbs} \quad \frac{16 \text{ oz}}{1 \text{ lbs}} \quad \frac{0.0283 \text{ kg}}{1 \text{ oz}} \\ + \quad \text{? oz} \quad \frac{0.0283 \text{ kg}}{1 \text{ oz}} \end{array} = \text{? kg}$$

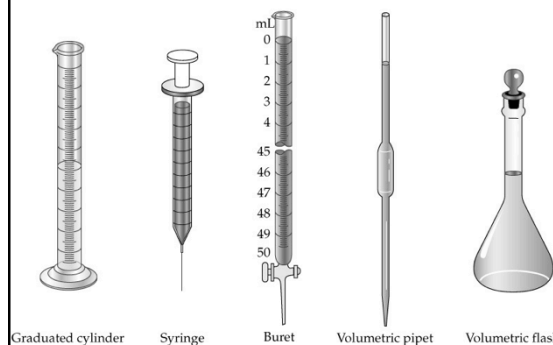


## Volume (Liquid Measurement Tools)

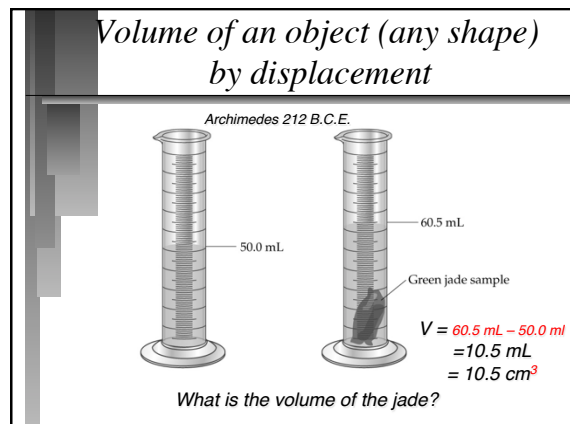
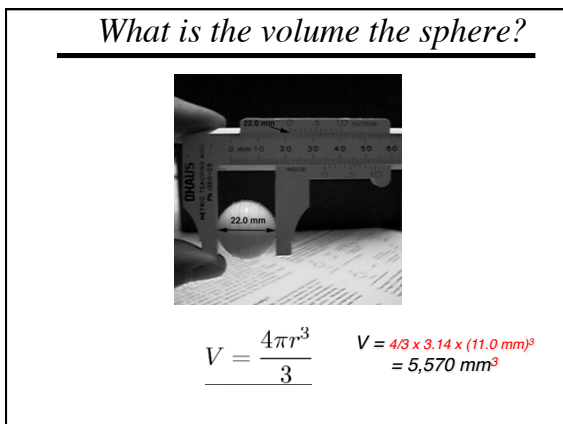
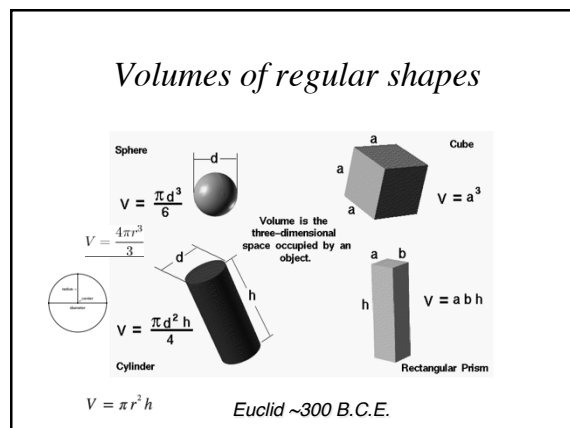
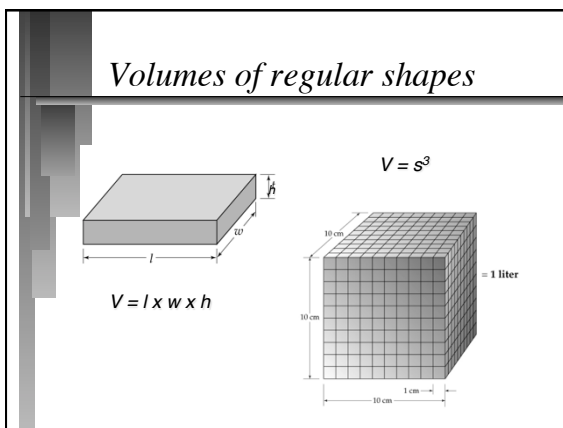
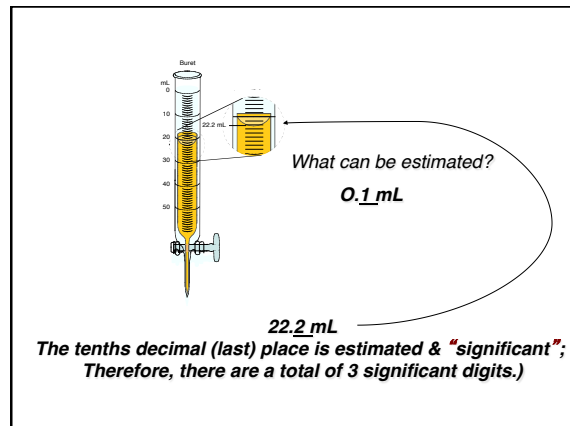
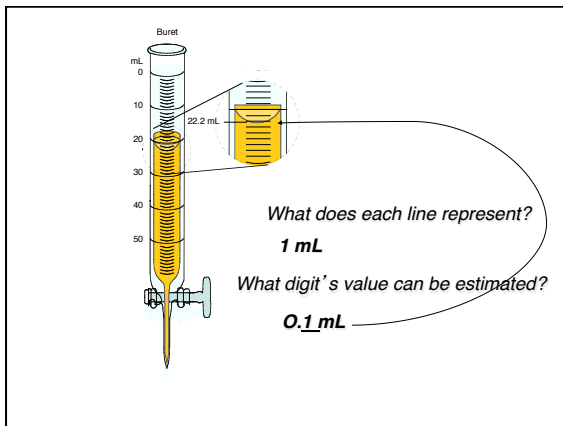


(CHEM 108)  
**METRIC UNITS:**  
milliliter

mL  
m = milli  
L = liter

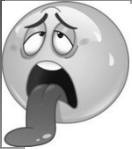


Volume UNITS: milliliter / mL / m = milli L = liter



**UNITS: Celsius (°C) & Kelvin (K)**

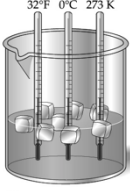
**Temperature is NOT Energy**



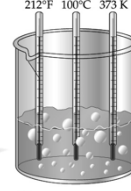
**“Temperature** (sometimes called **thermodynamic temperature**) is a measure of the average kinetic energy of the particles in a system. Adding heat to a system causes its **temperature** to rise.”

August. 15, 2015  
+142°F Manama,  
Bahrain

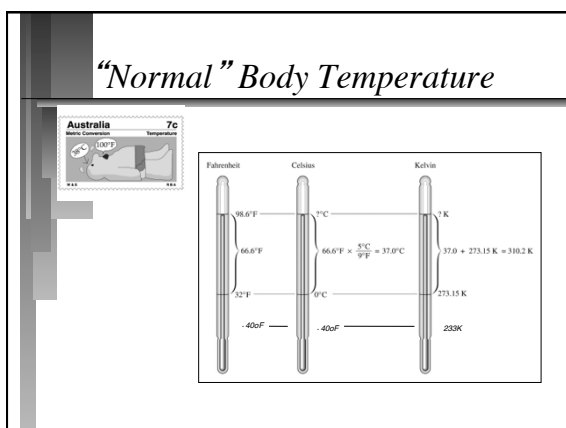
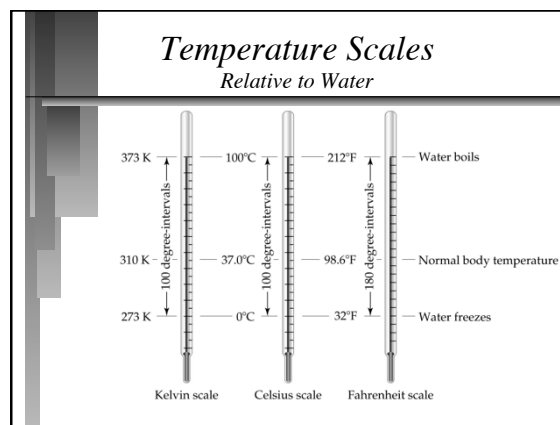
°C? = 61.7°C  
K? = 61.7°C + 273.15  
= 334.85 K



(a)



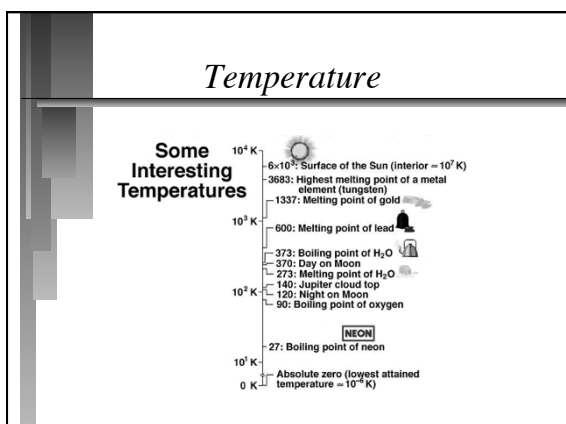
(b)



### QUESTION

Dr. R. walks into class and claims, “It is very cold in here today. It feels like 242 K.” If that were the temperature, would you agree that you would feel cold? What would that be in Celsius degrees?

- A. I agree, that would be 31°C.
- B. I agree, that would be – 31°C.
- C. I do not agree, that would be 31°C.
- D. I do not agree, that would be 515°C.



**QUESTION**

Identify the best match between the dimension or quantity and the unit that is most likely to be measured in Chem 108 lab.

	<u>Dimension or Quantity</u>	<u>Unit</u>
A)	Mass	Kilogram
B)	Length	Meter
C)	Volume	Milliliter
D)	Temperature	Fahrenheit
E)	Amount of substance	Megamole

## Commonly Used Prefixes in Chemistry

Metric Prefixes		
Prefix	Symbol	Multiple/Fraction
giga-	G	$1,000,000,000 = 1 \times 10^9$
mega-	M	$1,000,000 = 1 \times 10^6$
kilo-	k	$1,000 = 1 \times 10^3$
Basic unit: meter, gram, liter, second		
deci-	d	$0.1 = 1 \times 10^{-1}$
centi-	c	$0.01 = 1 \times 10^{-2}$
milli-	m	$0.001 = 1 \times 10^{-3}$
micro-	$\mu$	$0.000\,001 = 1 \times 10^{-6}$
nano-	n	$0.000\,000\,001 = 1 \times 10^{-9}$

## QUESTION

Select the correct relationship between these metric units of length or distance.

- A)  $1 \text{ km} = 100 \text{ m}$       B)  $1 \text{ mm} = 10 \text{ cm}$   
 C)  $1 \text{ nm} = 10^9 \text{ m}$       D)  $10^3 \text{ mm} = 1 \text{ m}$

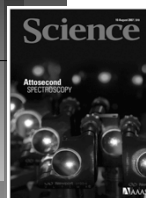
## QUESTION

Coincidentally, a U.S. nickel has a mass of approximately 5 grams. If you had one dollar's worth of nickels in your jean's what would be the mass of the nickels in milligrams?

- A. 100 milligrams  
 B. 50 milligrams  
 C. 1,000 milligrams  
 D. 100,000 milligrams

$$1000 \text{ milligrams (mg)} = 1 \text{ gram (g)}$$

## QUESTION



Science, 317, 765-775, (2007)  
 "The Electron Stopwatch"

An array of multilayer mirrors compresses ultrabroadband laser pulses (orange beam). The attosecond x-ray pulses allow the real-time observation of atomic-scale electron motion. The previous spectroscopic method was on a femtosecond scale, which was too slow to capture the movement.

How many times faster is attosecond spectroscopy compared to femtosecond methods?

- A. 10x B. 100x      C. 1,000x      D. 1,000,000x



Science, 317, 765-775, (2007)  
 "The Electron Stopwatch"

## QUESTION

How many times faster is attosecond spectroscopy compared to femtosecond methods?

Table: SI prefixes					
Factor	Name	Symbol	Factor	Name	Symbol
$10^{24}$	yocta	Y	$10^{-1}$	deci	d
$10^{21}$	zetta	Z	$10^{-2}$	centi	c
$10^{18}$	exa	E	$10^{-3}$	milli	m
$10^{15}$	peta	P	$10^{-6}$	micro	$\mu$
$10^{12}$	tera	T	$10^{-9}$	nano	n
$10^9$	giga	G	$10^{-12}$	pico	p
$10^6$	mega	M	$10^{-15}$	femto	f
$10^3$	kilo	k	$10^{-18}$	atto	a
$10^2$	hecto	h	$10^{-21}$	zepto	z
$10^1$	deka	da	$10^{-24}$	yocto	y

- A. 10x B. 100x      C. 1,000x      D. 1,000,000x

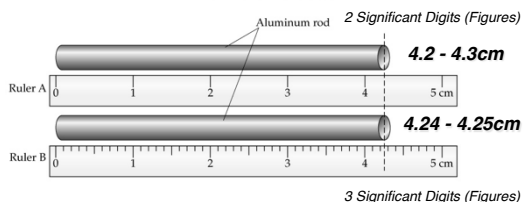
## Numbers

- Expressing a number correctly is determined by the method used in the measurement!
- How many numbers should I include?  
**Significant Digits (Figures)**  
 Consider: the exactness of the **measured** value
- Short Hand expression translates the number to **Scientific Notation**



## What is the length of the rod?

Different measurement tools give different numbers:  
Which ruler is better?



## Reporting Numbers Rules for Significant Digits (Figures)

- Nonzero integers always count as significant figures.
- 3456 g has how many sig figs?  
• 4 sig figs.
- Expressed in scientific notation?  
 $3.456 \times 10^3 \text{ g}$

## Reporting Numbers Rules for Significant (Digits) Figures

- Exact numbers (unit, conversion or scale factors) can have an infinite number of significant figures.
- 1 liter = 1,000. ml, exactly
- 1 inch = 2.54 cm, exactly

## Zeros

- Leading zeros do not count as significant figures.
- 0.0486 mL has how many sig figs?  
• 3 sig figs.
- Number expressed in scientific notation?  
 $4.86 \times 10^{-2} \text{ mL}$

## Zeros

- Captive zeros always count as significant figures.
- 16.07 cm has how many sig figs?  
• 4 sig figs.
- Number expressed in scientific notation?  
 $1.607 \times 10^1 \text{ cm}$

## Zeros

- Trailing zeros are significant only if the number contains a decimal point.
- 9.300 kg has how many sig figs?  
• 4 sig figs.
- Number expressed in scientific notation?  
 $9.300 \text{ kg}$

### QUESTION

In which of these measured values are the zeros not significant figures?

- I) 0.0591 cm
- II) 504 g
- III) 2.70 m
- IV) 5300 L

- A) I and II
- B) II and III
- C) I and IV
- D) I, III, and IV
- E) II, III, and IV

### QUESTION

Which one of the following does NOT represent four significant digits?

- A. 0.07100 mg
- B. 0.7100 mg
- C. 0.7010 mg
- D. 0.0710 mg

### Mathematics & Arithmetic

- Relative to method(s) of measurement
- Short Hand expression: Scientific Notation
- Numbers : How many to include?
  - Quantitative vs. Qualitative
- Addition/Subtraction.....
- Multiplication/Division.....
- What is "significant"?.....Rounding Off
- <http://www.chemteam.info/SigFigs/SigFigsFable.html>



### Computational Rules

- Addition/Subtraction: Answer expressed to the least number of decimal places of the figures in the process
- Multiplication/Division: Answer expressed to the least number of significant figures



### Computational Rules

#### Rules for Rounding Off:

- When numbers are used in a calculation, the result is rounded to reflect the significant figures of the *data*.
- For calculations involving multiple steps, only the final answer is only rounded—**NO rounding between steps**.

This prevents small rounding errors being magnified in the final answer.

- Use only the last (or leftmost) digit being dropped to decide how to round—ignore all digits to the right of it.
- The last number to be reported remains the same if the neighboring digit to be dropped is 4 or less; rounded up if the neighboring digit is 5 or more.

### Computational Rules

#### Addition and Subtraction Rule:

In addition or subtraction, the reported result has the same number of decimal places as the number with the fewest decimal places.

$$\begin{array}{r} 5.74 \\ 0.823 \\ + 2.651 \\ \hline 9.214 = 9.21 \end{array}$$

It is sometimes helpful to draw a vertical line directly to the right of the number with the fewest decimal places. The line shows the number of decimal places that should be in the answer.

$$\begin{array}{r} 4.8 \\ - 3.965 \\ \hline 0.835 = 0.8 \end{array}$$

## Addition

- 8 Four students were each asked to measure different pieces of wire and provide a total length for the four pieces.
- 8 Report the result correctly:

	0.05 cm
	12.01 cm
	1.9 cm
+	2.386 cm
	<hr/>
	16.346 cm

## QUESTION

If you were unloading a 23.50 kg box of books from your car and a "friend" added two more 482 gram chemistry books, how much in kg using the rules for significant digits, would you be lifting?

- A. 23.98 kg  
B. 24.464 kg  
C. 24.46 kg  
D. 24.5 kg

## Computational Rules

### Multiplication and Division Rule:

The result of multiplication or division carries the same number of significant figures as the factor with the fewest significant figures.

$$5.02 \times 89.665 \times 0.10 = 45.0118 = 45$$

(3 sig. figures) (5 sig. figures) (2 sig. figures) (2 sig. figures)

$$5.892 \div 6.10 = 0.96590 = 0.966$$

(4 sig. figures) (3 sig. figures) (3 sig. figures)

## Computational Rules

In calculations involving both multiplication/division and addition/subtraction, do any steps in parentheses first; determine the correct number of significant figures in the intermediate answer without rounding; then do the remaining steps.

$$3.489 \text{ cm} \times (5.67 \text{ cm} - 2.3 \text{ cm}) = ?$$

$$5.67 \text{ cm} - 2.3 \text{ cm} = 3.37 \text{ cm}$$

Use the subtraction rule to determine that the intermediate answer has only one significant decimal place. Do not round; underline the least significant figure as a reminder.

$$3.489 \text{ cm} \times 3.\underline{37} \text{ cm} = 11.758 \text{ cm}^2 = 12 \text{ cm}^2$$

Use the multiplication rule to determine that the intermediate answer (11.758) rounds to two significant figures (12) because it is limited by the two significant figures in 3.37.

## Mathematical Processes:

- 8 Provide correct answers assuming each value (unit omitted) is written with the correct number of significant figures:

$$\begin{array}{r} 12.01 \times 1.90 \\ \hline 2.386 \end{array} = 9.56370$$

$$\begin{array}{r} 12.01 \times 1.90 \\ \hline 2.386 \end{array} + 0.05 = 9.61370$$

## QUESTION

The average mass of a certain brand of vitamin C tablets is 253 mg. What is the mass of three such tablets rounded to the proper number of significant digits?

- A. 0.760 grams  
B. 0.759 grams  
C. 0.7590 grams  
D. 0.253 grams



## Systematic Problem Solving

### Dimensional/Unit Analysis: Conversions

#### Workshop



How many mL of milk are in a 1/2 gallon carton?

$$\begin{array}{ccc}
 0.50 \text{ gal} & \longrightarrow & ? \text{ mL} \\
 \downarrow & & \downarrow \\
 1 \text{ gal} = 4 \text{ qt} & \longrightarrow & 1 \text{ qt} = 946 \text{ mL} \\
 \hline
 \frac{0.50 \text{ gal}}{1 \text{ gal}} \times \frac{4 \text{ qt}}{1 \text{ gal}} \times \frac{946 \text{ mL}}{1 \text{ qt}} = ? \text{ mL}
 \end{array}$$

## Complete the following

### Units & Conversions

Number	Scientific Notation	Named unit
13,000,000,000 yrs.	$1.3 \times 10^{10} \text{ yrs}$	? <u>gigayears</u> 13 Gyrs
546 mL	$5.46 \times 10^2 \text{ mL}$	0.546 Liters 0.546 L
0.845 kg	$8.45 \times 10^{-1} \text{ kg}$	? <u>grams</u> 845 g

## QUESTION

### General Chemistry Level Challenge



In 1999, NASA lost the \$125 million Mars Climate Orbiter, when it mistakenly was sent to come within 37 miles from Mars' surface, which took it far into the Martian atmosphere where friction caused it to burn and break apart. The failed plan had been to place it in an orbit 142 miles above Mars where the atmosphere is thinner.

## QUESTION

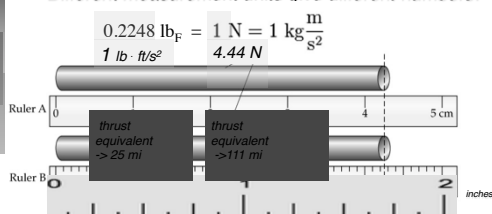
### General Chemistry Level Challenge



- The problem was caused by a navigation error from different calculations & communications between two computer programs, one using English units for force (pounds of force), and the other using metric units (Newtons), which are numerically more than 4 times larger than the pound of force unit.

## Comparing Distances (length)

Different measurement units give different numbers:



.....navigating thrust and distance for the Mars Climate Orbiter

## QUESTION

### General Chemistry Level Challenge



- One NASA program specified navigation of the Climate Orbiter to a distance of  $7.55 \times 10^5 \text{ ft}$  from the surface, while the second program using this value as a unitless number calculated thrust in Newtons that took it to  $5.95 \times 10^4 \text{ m}$
- What is the difference in kilometers between the two altitudes?

## Numbers & Measurement

### Units & Conversions



Crash Course: Hank & John Green  
Unit Conversion & Significant Figures:  
<https://www.youtube.com/watch?v=hQpQ0hxVNTg&list=PL8dPuuaLjXtPHzzYuWy6fYEaX9mQQ8oGr&index=2>, 11:23 min/sec

## Calculations / Computations

### Fastest computer (2001): 12 TeraFLOPS/second

TI-Graphing  
6 Ghz  
Cost  $\approx$  \$100  
(2001 dollars)

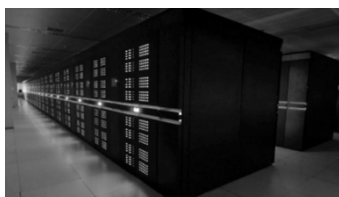
Tera- =  $10^{12}$  (trillion)  
Cost =  $\sim$  \$30,000,000 (2001 dollars)  
<http://www.llnl.gov/asci-scrapbook/>



## World's fastest computers (2017)

<https://www.youtube.com/watch?v=KEdsrT1mFAU>

Peta- =  $10^{15}$  (quadrillion); 1,000 trillion



Sunway TaihuLight (93 PetaFLOPS), China  
Tianhe-2, aka Milky Way (33.9 PetaFLOPS), China  
Estimated Costs: >\$100 million (2016 dollars)

## Floating Point Operations (FLOPS)

Equivalent to adding one plus one

- When told to begin, count 1+1.
- Keep repeating the counting of 1+1 and keep track of how many times that you have repeated 1+1.
- Stop when told to, note your total.

<https://www.youtube.com/watch?v=DsXXjMhHMVg>

## Floating Point Operations

### FLOPS

- There are about 60 of us here. The estimated processing power/min for our group is: \_\_\_\_\_. The median for our group is: \_\_\_\_\_ (Average vs. Median?)
  - This is equal to how many FLOPS (Floating point Operations/ sec.)?
  - How many people would be needed to produce 1 petaFLOP (i.e. adding 1+1 one quadrillion [ $1 \times 10^{15}$ ] times)? \_\_\_\_\_
  - In 2018, the estimated population of the U.S. is 327 million people, the world population estimated at 7.3 billion. How many of these respective U.S. populations and world populations are needed to do the work of the world's fastest computer (93 petaFLOPS)?
  - U.S. \_\_\_\_\_ World \_\_\_\_\_
- $$(93 \times 10^{15} \text{ FLOPS} / 327 \times 10^6 \text{ persons}) \times 1 \text{ person} / 1 \text{ FLOP} =$$
  
$$/ 7.3 \times 10^6 \text{ persons}$$

## General Chemistry Level Challenge

### Measurements: Scaling/ Problem Solving

### Powers of Ten (Exponents: $10^x$ )

- Scaling: U.S. Population in 2003 vs. 2018
  - 1 birth every 12 seconds (2003) vs. 8 seconds (2018)
  - 1 death every 20 seconds (2003) vs. 10 seconds in (2018)
  - 1 new immigrant every 21 s (2003) vs. 29 s (1/2018)
- Considering the data, what is the net effect on the U.S. population in 2018.... Is it growing or declining? .... faster or slower than 2003? ... by what percent vs. 2003?
- The U.S. census population was 321,442,019 on July 4, 2015. Calculate what it is today considering the data.
- KEY: How many seconds from July 4, 2015 to February 1, 2018?