

Chemistry & STEM Measurement II

Discussion Guide 1.4

Density

An Objects' Relationship of its Mass & Volume

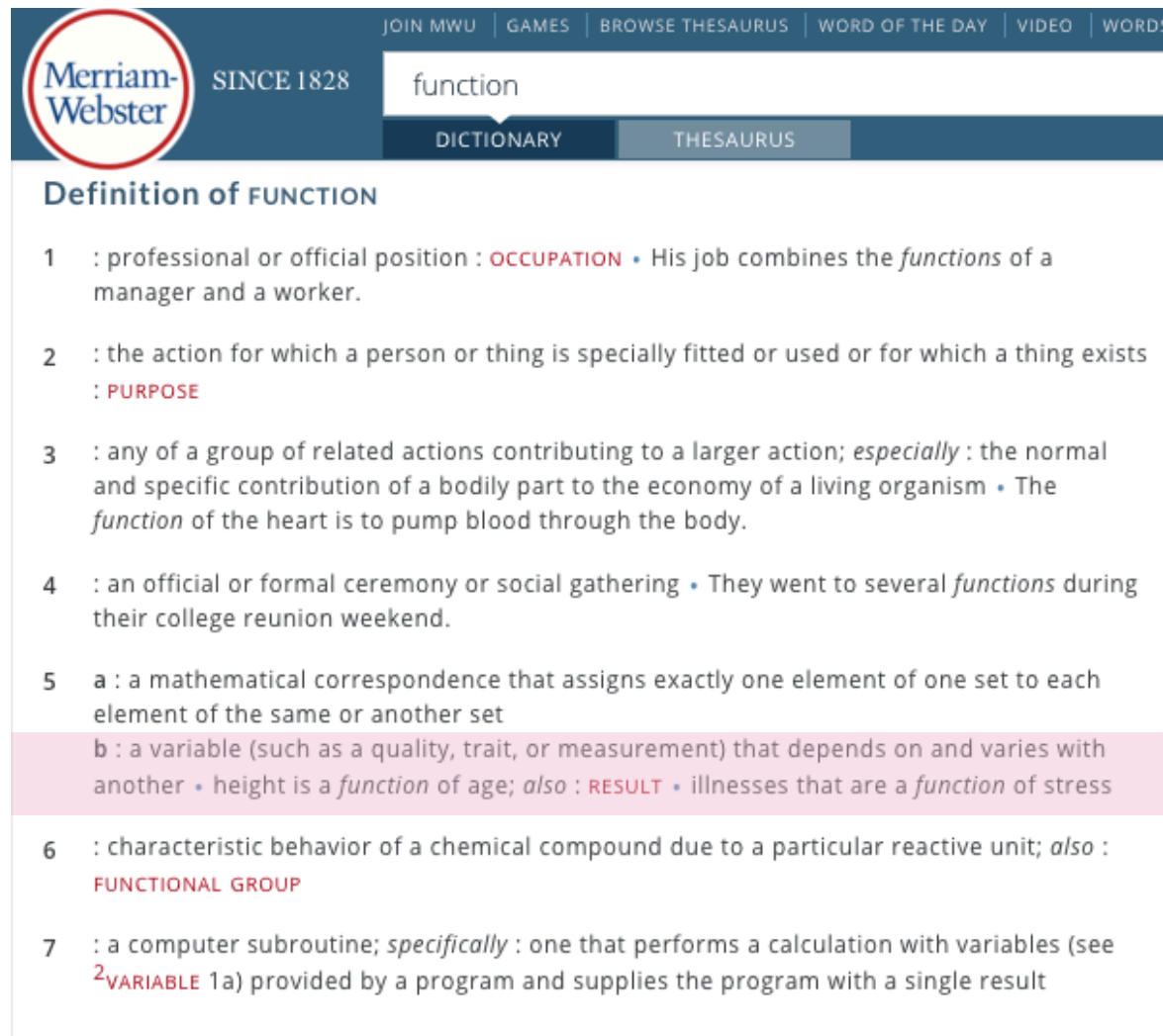
Dr. Ron Rusay



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Comparison of Relative Properties

FUNCTIONS



The image shows a screenshot of the Merriam-Webster website. The header includes the Merriam-Webster logo, 'SINCE 1828', and navigation links: 'JOIN MWU', 'GAMES', 'BROWSE THESAURUS', 'WORD OF THE DAY', 'VIDEO', and 'WORDS'. A search bar contains the word 'function'. Below the search bar are tabs for 'DICTIONARY' and 'THESAURUS'. The 'DICTIONARY' tab is selected, showing the 'Definition of FUNCTION'. The definition is a numbered list of seven items. Item 5 is highlighted with a pink background. Item 5a is a mathematical definition, and item 5b is a general definition of a variable. Item 6 is a definition for chemistry. Item 7 is a definition for computer science.

Merriam-Webster SINCE 1828

function

DICTIONARY THESAURUS

Definition of FUNCTION

- 1 : professional or official position : **OCCUPATION** • His job combines the *functions* of a manager and a worker.
- 2 : the action for which a person or thing is specially fitted or used or for which a thing exists : **PURPOSE**
- 3 : any of a group of related actions contributing to a larger action; *especially* : the normal and specific contribution of a bodily part to the economy of a living organism • The *function* of the heart is to pump blood through the body.
- 4 : an official or formal ceremony or social gathering • They went to several *functions* during their college reunion weekend.
- 5 a : a mathematical correspondence that assigns exactly one element of one set to each element of the same or another set
b : a variable (such as a quality, trait, or measurement) that depends on and varies with another • height is a *function* of age; *also* : **RESULT** • illnesses that are a *function* of stress
- 6 : characteristic behavior of a chemical compound due to a particular reactive unit; *also* : **FUNCTIONAL GROUP**
- 7 : a computer subroutine; *specifically* : one that performs a calculation with variables (see ²**VARIABLE** 1a) provided by a program and supplies the program with a single result

Density is a function of an object's mass and volume.

Comparison of Relative Properties

FUNCTIONS

About 481,000,000 results (0.66 seconds)

Function (mathematics) - Wikipedia

[https://en.wikipedia.org/wiki/Function_\(mathematics\)](https://en.wikipedia.org/wiki/Function_(mathematics)) ▼

In mathematics, a **function** is a relation between a set of inputs and a set of permissible outputs with

the property th

real number x

Graph of a fun



Filters ▼

Function |

www.dictiona

A relationship

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Composite fu

TYPES
OF
FUNCTIONS

types of functions|

types of functions and their graphs

types of functions in c language

types of functions

types of functions khan academy

types of functions in discrete mathematics

types of functions in javascript

types of functions song

types of functions in sql

types of functions in python

types of functions calculus

What is a function? (video) | Functions | Khan Academy



<https://www.khanacademy.org/...functions/...functions/.../what-is-...> ▼

Uploaded by Khan Academy

Functions assign a single unique output for each of their inputs. In this video, we see examples of various kinds ...

Functions | Algebra I | Math | Khan Academy

<https://www.khanacademy.org/math/algebra/algebra-functions> ▼

Functions are mathematical entities that assign unique outputs to given inputs. Sounds simple? Think again! In this topic you will evaluate, graph, analyze, and create various types of **functions**.

Comparisons of Relative Properties

FUNCTIONS

Example: density : mass : volume

Functions & variables can be described interchangeably between:

- 1) Images (Symbols)*
- 2) Words*
- 3) Sounds (Voice)*
- 4) Numbers*
- 5) Tables*
- 6) Graphs*
- 7) Formulas*



Mass



Volume

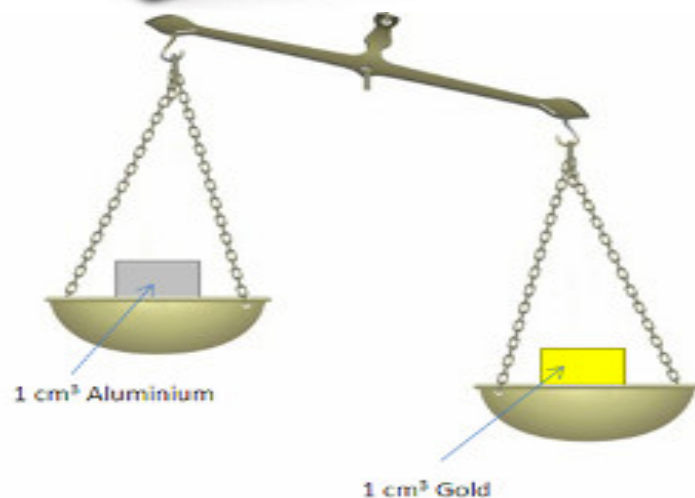
Density

Density is a function of an object's mass and volume.

Density

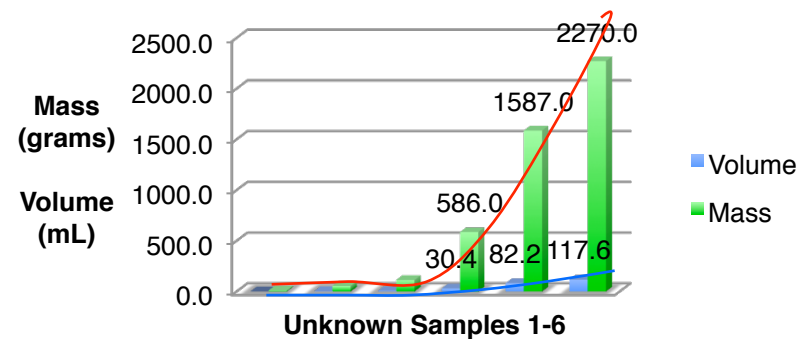
Mass & Volume

Numbers
Tables
Graphs

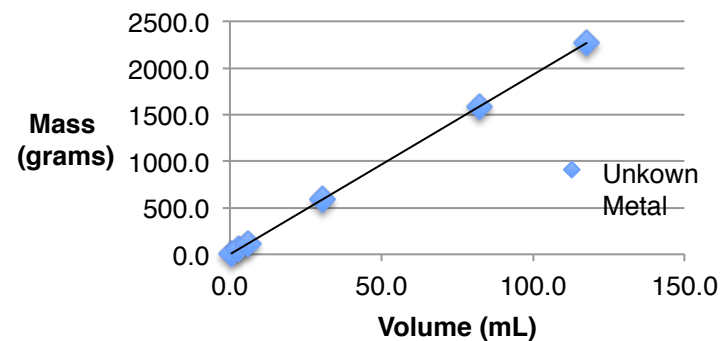


Metal

Mass & Volume



Density



Numbers, Tables, & Graphs

Density

Formulas

<http://www.density.com/what.htm>

Density = Mass / Volume [g/mL or g/cm³; g/L]

The diagram illustrates the density formula $d = \frac{m}{V}$ with numerical values. A callout box labeled "mass (m)" points to the numerator "156 g". Another callout box labeled "volume (V)" points to the denominator "20.0 cm³". A third callout box labeled "density (d)" points to the result "7.80 g/cm³".

$$d = \frac{m}{V} = \frac{156 \text{ g}}{20.0 \text{ cm}^3} = 7.80 \text{ g/cm}^3$$

Archimedes 250 B.C.E. Does iron float?.... The RMS Titanic?

Density

<http://www.density.com/what.htm>

Archimedes 250 B.C.E. Does iron float?.... The RMS Titanic?

NOVA: The Secrets of Archimedes

<https://www.youtube.com/watch?v=0n347dxm5uE>

NOVA: Why Do Ships Sink?

https://www.youtube.com/watch?v=n_xDZjrZ6zs

Density

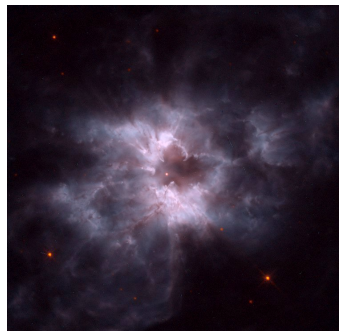
Density = Mass / Volume [g/mL or g/cm³; g/L] (kg/m³)

Very Dense Astronomical Objects: White Dwarfs

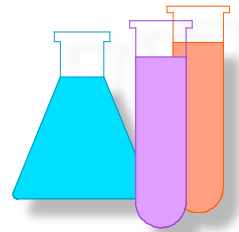
<http://antwarp.gsfc.nasa.gov/apod/ap961203.html>

$$\begin{aligned} D(\rho) &= 1 \times 10^9 \text{ kg/m}^3 = 1 \times 10^3 \text{ kg/cm}^3 \\ &= 1 \times 10^6 \text{ g/cm}^3 \end{aligned}$$

A White Dwarf's mass is comparable to our Sun's, but its volume is about a million times smaller; the average density is ~1,000,000 times greater than the Sun's 1.4 kg/m³



Our Sun will eventually become a white dwarf “butterfly”..... but not for ~5 billion years.

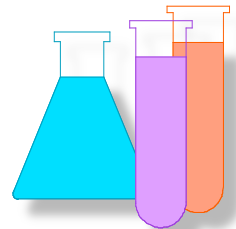


Dimensional Analysis

Conversion/Unit Factor Calculations

- Using exact numbers / “*scale factors*” UNITS
- A Bookkeeping Process: Example
Calculating the density [$D(\rho) = ? \text{ g/cm}^3$] of a white dwarf,
 $1.0 \times 10^9 \text{ kg} / 1 \text{ m}^3$
- (**$1 \text{ kg} = 1000\text{g}$; $1 \text{ m}^3 = 1 \times 10^6 \text{ cm}^3$; $1 \text{ Ton (T)} = 1000\text{kg}$**)

$$\frac{\text{kg}}{\text{m}^3} \times \frac{\text{m}^3}{\text{cm}^3} \times \frac{\text{g}}{\text{kg}} = \frac{? \text{ g}}{? \text{ cm}^3}$$



Dimensional Analysis

Conversion/Unit Factor Calculations

- Using exact numbers / “*scale factors*” UNITS

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Calculating the density [$D(\rho) = ? \text{ g/cm}^3$] of a white dwarf,
 $1.0 \times 10^9 \text{ kg} / 1 \text{ m}^3$

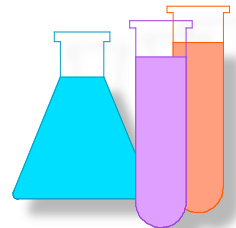
- ($1 \text{ kg} = 1000\text{g}$; $1 \text{ m}^3 = 1 \times 10^6 \text{ cm}^3$; $1 \text{ Ton (T)} = 1000\text{kg}$)

$$\begin{array}{c|c|c}
 1.0 \times 10^9 & & \\
 \hline
 \text{kg} & \text{m}^3 & \text{g} \\
 \hline
 1 \text{ m}^3 & \text{cm}^3 & \text{kg}
 \end{array}
 = \frac{? \text{ g}}{? \text{ cm}^3}$$

$1,000,000 = 1.0 \times 10^6$

1

$1.000 \times 10^6 = (100 \text{ cm})^3$

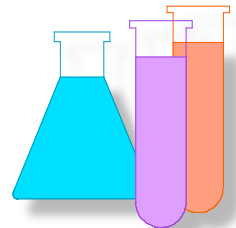


Dimensional Analysis

Continued

- *Example for an astronomical object where 1 teaspoon weighs 3 Tons. (~ 3 pick up trucks).*
 $3\ T / 1\ tsp \longrightarrow ?\ g/cm^3$
- *(1 tsp = 4.9289 mL; 1 T (Ton) = 1,000 kg; 1 kg = 1,000 g; 1 mL = 1 cm³)*

T	tsp	mL	kg	g	$=$	$? g$
tsp	mL	cm^3	T	kg		$? cm^3$



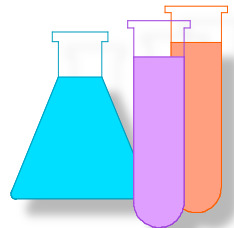
Dimensional Analysis

Continued

- Example for an astronomical object where 1 teaspoon weighs 3 Tons. (~ 3 pick up trucks).
 $3 \text{ T} / 1 \text{ tsp} \longrightarrow ? \text{ g/cm}^3$
- ($1 \text{ tsp} = 4.9289 \text{ mL}$; $1 \text{ T (Ton)} = 1,000 \text{ kg}$; $1 \text{ kg} = 1,000 \text{ g}$; $1 \text{ mL} = 1 \text{ cm}^3$)

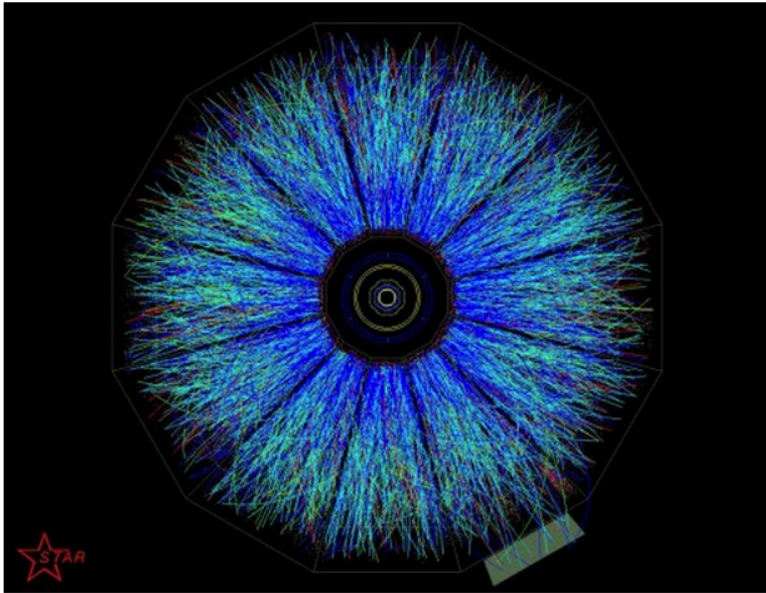
3 T	1 tsp	1 mL	$1.000 \times 10^3 \text{ kg}$	$1.000 \times 10^3 \text{ g}$	$=$	$? \text{ g}$
1 tsp	4.9289 mL	1 cm^3	1 T	1 kg		$? \text{ cm}^3$

$6 \times 10^5 \text{ g/cm}^3$



Density

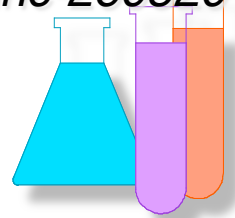
Density = Mass / Volume [g/mL or g/cm³; g/L; kg/m³]



Known as the quark-gluon plasma, this amazing **exotic substance** can exist only at incredibly high temperatures or pressures, and it consists almost entirely of free quarks and gluons; it is possible that the whole universe was filled only with this substance in the immediate aftermath of the Big Bang.

“Besides black holes, there’s nothing denser than what we’re creating,” said David Evans, a team leader for the Large Hadron Collider’s ALICE detector, which helped observe the quark-gluon plasma shown. “If you had a cubic centimeter of this stuff, it would weigh 40 billion tons.”

<http://www.zmescience.com/science/physics/quark-gluon-plasma-lhc-26052011/#ixzz3foandtPt>



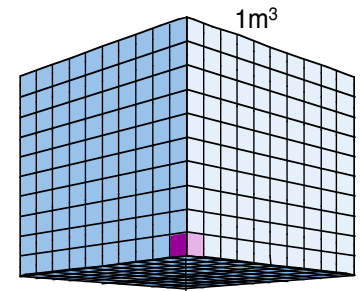
How does quark-gluon plasma’s density compare to a white dwarf? (1 ton = 1,000 kg)

Calculate the density [$D(\rho) = ?$] ($\text{kg}/\text{cm}^3 \dots \text{or } \text{g}/\text{cm}^3 \dots \text{or } \text{kg}/\text{m}^3$)
of quark-gluon plasma: 1 cm^3 has a mass of $4.0 \times 10^{10} \text{ T}$
(metric tons) **4.0×10^{10} greater**
for comparison to **White Dwarf**.

($1 \text{ T} = 1,000 \text{ kg}$; $1 \text{ kg} = 1,000 \text{ g}$; $1,000,000 \text{ cm}^3 = 1 \text{ m}^3$)

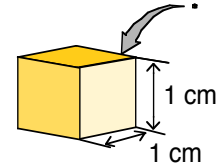
$4.0 \times 10^{10} \text{ T}$	$1,000 \text{ kg}$	$= 4.0 \times 10^{13} \text{ kg}/\text{cm}^3$ $1 \times 10^3 \text{ kg}/\text{cm}^3$
cm^3	T	

$4.0 \times 10^{10} \text{ T}$	$1,000 \text{ kg}$	$1,000 \text{ g}$	$= 4.0 \times 10^{16} \text{ g}/\text{cm}^3$ $1 \times 10^6 \text{ g}/\text{cm}^3$
cm^3	T	kg	



$1 \text{ dm}^3 = 1 \text{ L}$

$1 \text{ cm}^3 = 1 \text{ mL}$



$4.0 \times 10^{13} \text{ kg}$	$1,000,000 \text{ cm}^3$	$= 4.0 \times 10^{19} \text{ kg}/\text{m}^3$ $1 \times 10^9 \text{ kg}/\text{m}^3$
cm^3	m^3	

Density: Ultralight microlattices

Density = Mass / Volume [g/mL or g/cm³; g/L; kg/m³]

T. A. Schaedler et al. Science 2011;334:962-965



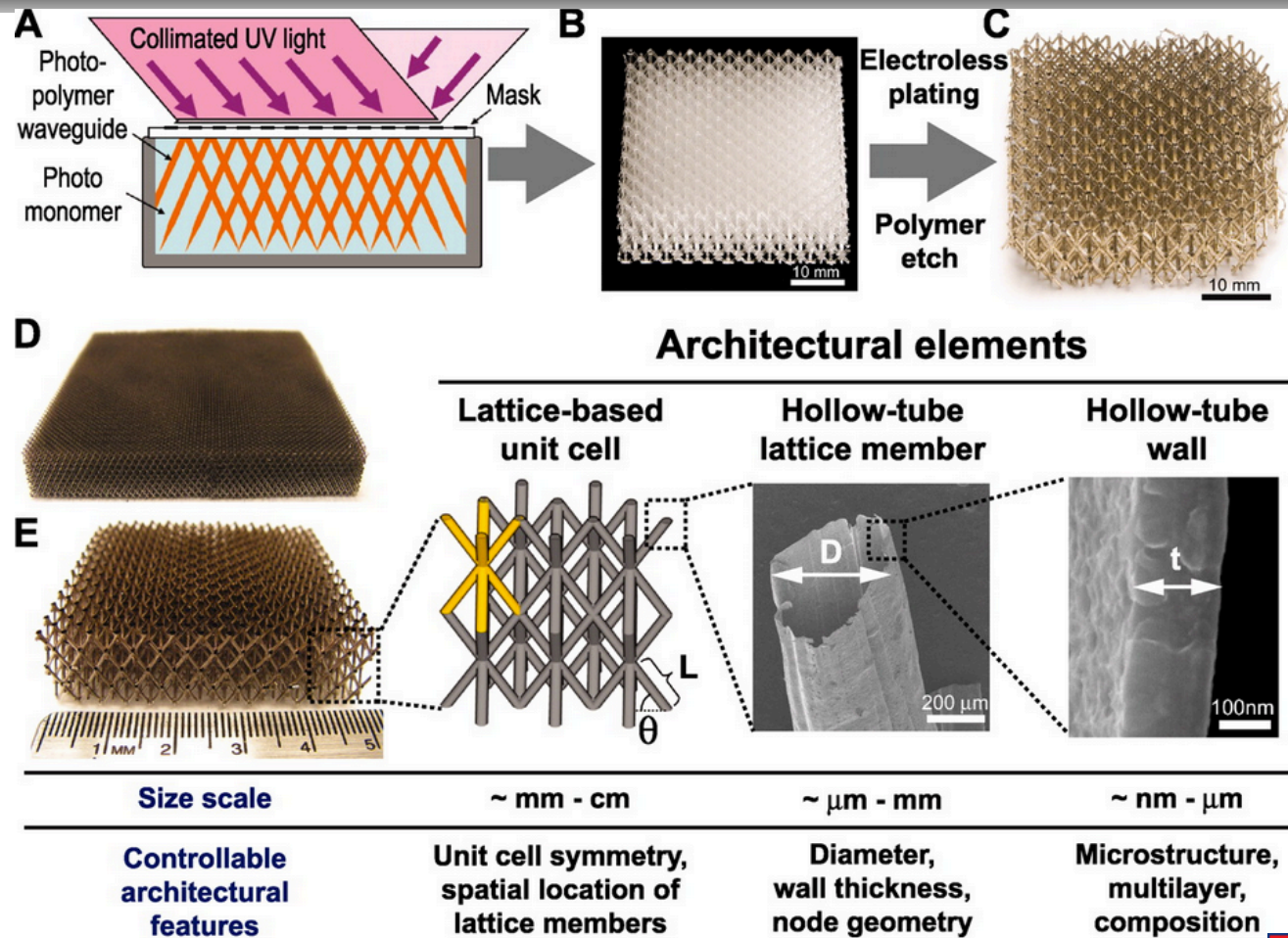
<http://www.gizmag.com/ultralight-micro-lattice-material/20537/>

0.9 mg/cm³ (air = 1.2 mg/cm³)

Engineering Ultralight Microlattices

Density = Mass / Volume [g/mL or g/cm³; g/L; kg/m³]

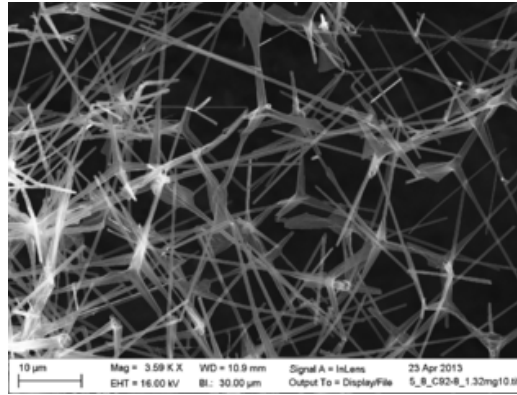
T. A. Schaedler et al. Science 2011;334:962-965



0.9 mg/cm³

Density

Density = Mass / Volume [g/mL or g/cm³; g/L; kg/m³]



- *Aerographite is a synthetic foam consisting of a porous interconnected network of carbon nanotubes. It was first reported by researchers at the University of Kiel and the Technical University of Hamburg in Germany in a scientific journal in June 2012. It's density is:*
- *$D = 0.18 \text{ mg/cm}^3$*

Density

Density = Mass / Volume [g/mL or g/cm³; g/L; kg/m³]

<https://www.youtube.com/watch?v=3bIXUBXj070>



0.16 mg/cm³

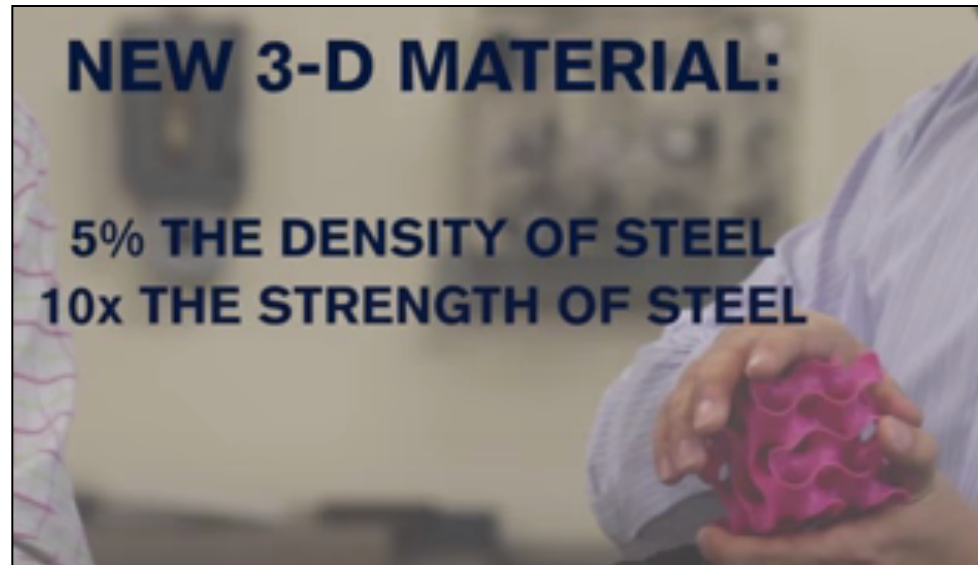
The graphene aerogel can be supported by blades of grass

*Chao Gao et. al., Zhejiang University, Department of
Polymer Science and Engineering
Nature 494, 404 (28 February 2013)
doi:10.1038/494404a*

Density

Density = Mass / Volume [g/mL or g/cm³; g/L; kg/m³]

<https://www.youtube.com/watch?v=VlcZdc42F0g>



NEW 3-D MATERIAL:

**5% THE DENSITY OF STEEL
10x THE STRENGTH OF STEEL**

Structural 3-D Graphene

One of the strongest lightweight materials known

MIT: January 2017

QUESTION

A metal sample is hammered into a rectangular sheet with an area of 31.2 ft^2 and an average thickness of $2.30 \times 10^{-6} \text{ cm}$. If the mass of this sample is 0.4767 g , predict the identity of the metal.

The density of the metal is shown in parenthesis.

Useful information: $1 \text{ ft}^2 = 929 \text{ cm}^2$



A) Aluminum (2.70 g/cm^3)

B) Copper (8.95 g/cm^3)

C) Gold (19.3 g/cm^3)

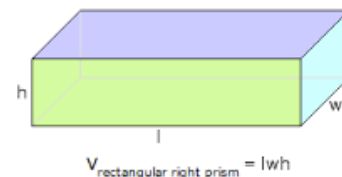
D) Zinc (7.15 g/cm^3)

Set up a dimensional analysis path to solve the problem

Dimensional Analysis

A metal sample is hammered into a rectangular sheet with an area of 31.2 ft^2 and an average thickness of $2.30 \times 10^{-6} \text{ cm}$. If the mass of this sample is 0.4767 g , predict the identity of the metal.

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A) Aluminum (2.70 g/cm^3)

B) Copper (8.95 g/cm^3)

C) Gold (19.3 g/cm^3)

D) Zinc (7.15 g/cm^3)

What goes in here?

31.2 ft^2	$\frac{1}{929}$	$\frac{\text{ft}^2}{\text{cm}^2}$	$\frac{0.4767 \text{ g}}{2.30 \times 10^{-6} \text{ cm}}$	$=$	$\frac{? \text{ g}}{? \text{ cm}^3}$
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QUESTION

A metal sample is hammered into a rectangular sheet with an area of 31.2 ft^2 and an average thickness of $2.30 \times 10^{-6} \text{ cm}$. If the mass of this sample is 0.4767 g , predict the identity of the metal.

The density of the metal is shown in parenthesis.

Useful information: $1 \text{ ft} = 12 \text{ in}$; $1 \text{ in} = 2.54 \text{ cm}$

A) Aluminum (2.70 g/cm^3)

B) Copper (8.95 g/cm^3)

C) Gold (19.3 g/cm^3)

D) Zinc (7.15 g/cm^3)

Dimensional Analysis

Solved in 2 Steps

A metal sample is hammered into a rectangular sheet with an area of 31.2 ft^2 and an average thickness of $2.30 \times 10^{-6} \text{ cm}$. If the mass of this sample is 0.4767 g , predict the identity of the metal.

ø The density of the metal is shown in parenthesis.

ø Useful information: $1 \text{ ft} = 12 \text{ in}$; $1 \text{ in} = 2.54 \text{ cm}$

ft^2	in^2	cm^2	cm	$=$	$? \text{ cm}^3$
	ft^2	in^2			

*Densities of Various Common Substances**

Densities of Various Common Substances* at 20°C

Substance	Physical State	Density (g/cm³)
Oxygen	Gas	0.00133
Hydrogen	Gas	0.000084
Ethanol	Liquid	0.789
Benzene	Liquid	0.880
Water	Liquid	0.9982
Magnesium	Solid	1.74
Salt (sodium chloride)	Solid	2.16
Aluminum	Solid	2.70
Iron	Solid	7.87
Copper	Solid	8.96
Silver	Solid	10.5
Lead	Solid	11.34
Mercury	Liquid	13.6
Gold	Solid	19.32

*At 1 atmosphere pressure

QUESTION

Which would provide more grams of NaCl, sample one with a mass of 2,350 mg, or sample two, a solid with a volume of 2.00 cm³? (The density of solid salt is 2.16 g/cm³.) Select the most massive sample and its mass in grams.

- A. Sample two; 1.08 grams
- B. Sample two; 4.32 grams
- C. Sample one; 2.35 grams
- D. Sample one; 2.350 grams

QUESTION

The volume of any material can be obtained from its density and mass.

If the mass of a sample of acid from a battery were 5.00 grams and its density was 1.2 g/mL, what would the correct reported volume in mL with the proper number of significant digits?

- A. 6.0 mL
- B. 6.00 mL
- C. 4.2 mL
- D. 4.17 mL

Density

Density = Mass / Volume [g/mL or g/cm³; g/L]

Mass = Density x Volume

- *How many grams of air are there in PS 277?*

- *The room has dimensions of ~ 3.5 m x 11 m x 10. m.*

- *$D_{\text{air}} = 1.22 \times 10^{-3} \text{ g/cm}^3$ (1.22 g/L)*

- *$1 \text{ m}^3 = 100 \text{ cm} \times 100 \text{ cm} \times 100 \text{ cm};$*

- *$1000 \text{ cm}^3 = 1 \text{ L}; 1 \text{ mL} = 1 \text{ cm}^3$*

A. $1.22 \times 10^3 \text{ g}$

B. 385,000,000 g

C. $3.85 \times 10^6 \text{ g}$

D. 47,000,000 g

E. $4.70 \times 10^8 \text{ g}$



Dimensional Analysis

Conversion/Unit Factor Calculations

- How many grams of air are there in PS 277?
- The room has dimensions of $\sim 3.50 \text{ m} \times 11.0 \text{ m} \times 10.0 \text{ m} = 385 \text{ m}^3$
- $D_{\text{air}} = 1.22 \times 10^{-3} \text{ g/cm}^3$ (1.22 g/L)
- $1 \text{ m}^3 = 100 \text{ cm} \times 100 \text{ cm} \times 100 \text{ cm};$
- $1000 \text{ cm}^3 = 1 \text{ L}; 1 \text{ mL} = 1 \text{ cm}^3$

$$\begin{array}{c|c|c}
 385 \text{ m}^3 & \frac{1 \times 10^6}{\text{cm}^3} & \frac{1.22}{\text{g}} \\
 \hline
 & \frac{1}{\text{m}^3} & \frac{1}{\text{cm}^3}
 \end{array} =$$



QUESTION

Density

Density = Mass / Volume [g/mL or g/cm³; g/L]

*If the room were filled with pure oxygen,
 $D_{\text{oxygen}} = 1.429 \times 10^{-3} \text{ g/cm}^3$ (1.429 g/L)
there will be a higher mass of gas in the room.*

True (A) / False (B)

(Be able to explain the reason(s) for your answer.)



QUESTION

General Chemistry Level Challenge

How many pounds of air are there in PS 277?
It has a volume of $\sim 220 \text{ yd}^3$.

$$D_{\text{air}} = 1.22 \times 10^{-3} \text{ g/cm}^3 \text{ (1.22 g/L)}$$

Mass = Density x Volume

$$\text{Mass} = 450 \text{ lbs (451.996005)}$$

$220 \cancel{\text{yd}^3}$	$\frac{27}{\cancel{\text{ft}^3}}$	$\frac{28316.8}{\cancel{\text{cm}^3}}$	$\frac{0.00122}{\cancel{\text{g}}}$	$\frac{1}{\text{lb}}$	= ? lb
	$\frac{1}{\cancel{\text{yd}^3}}$	$\frac{1}{\cancel{\text{ft}^3}}$	$\frac{1}{\cancel{\text{cm}^3}}$	$\frac{454}{\cancel{\text{g}}}$	



QUESTION

General Chemistry Level Challenge



Titanium is abundant in the earth's crust, but horrendously difficult to turn into a bicycle frame. From extraction, to final welding and finishing, titanium is fraught with very complex processes that are as expensive as they are essential. One slip, omission on behalf of the mill, machinist, welder or finisher or the slightest contamination of oxygen, nitrogen, and hydrocarbon (i.e. human fingertips) at the wrong time and the frame will almost certainly fail at some point. Hence most bike companies don't use titanium.

<http://cyclefit.co.uk/journal/5-questions-to-ask-before-buying-a-titanium-bike>

QUESTION

General Chemistry Level Challenge



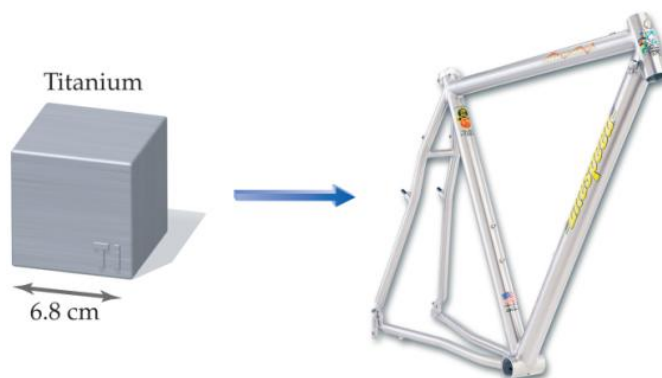
However, titanium's tolerance to cyclical load is infinite. This is a huge advantage both in terms of safety and for ride quality. It means that as long as the tube spec and frame design is well executed, a bicycle will offer exceptional comfort, performance and ride the same in its first mile as its millionth!

- ø *Titanium is much lighter than steel alloy, which has been commonly used in frames.*
- ø *Titanium (4.50 g/cm^3); steel alloy (7.75 g/cm^3).*

<http://cyclefit.co.uk/journal/5-questions-to-ask-before-buying-a-titanium-bike>

QUESTION

General Chemistry Level Challenge



\$4,199.00

- ø A titanium bicycle frame contains the same amount of titanium as a titanium cube measuring 6.8 cm on a side.
- ø Use the density of titanium to calculate the mass in kilograms of titanium in the frame.
- ø What would be the mass of a similar frame composed of steel alloy?

Titanium (4.50 g/cm³); Steel alloy (7.75 g/cm³).

\$9,000.00 frame

QUESTION

General Chemistry Level Challenge



- A stiff light weight carbon fiber bicycle frame is said to weigh as little as 690g.
- Carbon fiber frames are the mainstay of the Tour de France.



- What is the percent difference in the weight of a carbon fiber frame versus titanium?
- What is the relative cost per kg for each of them?
- Assuming the volume of carbon fiber in the frame is equal to titanium, what is the density of the carbon fiber?

QUESTION

General Chemistry Level Challenge

<http://chemconnections.org/general/chem108/3D%20printing%20transforms%20the%20economics%20of%20manufacturing.pdf>

<http://chemconnections.org/general/chem108/3D%20printers%20start%20to%20build%20factories%20of%20the%20future.pdf>

Weighty matters

	Value of weight saving, \$/kg
F1 motorsport	More than 120,000
Spacecraft	25,000
Aircraft	1,200-13,000
Automotive	20-600
Trucks, excavators, etc	1.3-12.7
Factory equipment	0-6

Source: Marcus Pont, Domin Fluid Power, 2017

Economist.com

Reducing weight offers large returns besides winning the Tour de France.

Read the linked articles above, and briefly explain how 3D printing relates to these savings in one or more of the examples from the table. Also, are there any opportunities in your chosen career path for 3D printing applications?